

# AME CET Mathematics

## Sample Paper – 2

Duration: 20 Minutes

Maximum Marks: 80

### Instructions

- This paper contains **20** Multiple Choice Questions (Single Correct Answer), modelled on the Mathematics section of **AME CET** entrance.
- Each correct answer carries **+4 marks**. Each wrong answer carries **-1 mark**. Unattempted questions carry **0 marks**.
- Only **one** option is correct per question. Choose carefully.
- Syllabus level: **Class 11 and 12 NCERT Mathematics** (Sets and Relations to Probability and Statistics).
- Use of mobile phones, calculators, or any electronic gadget is strictly prohibited.

**Q1.** The value of  $\int_0^{\pi/2} x \cos x \, dx$  is:

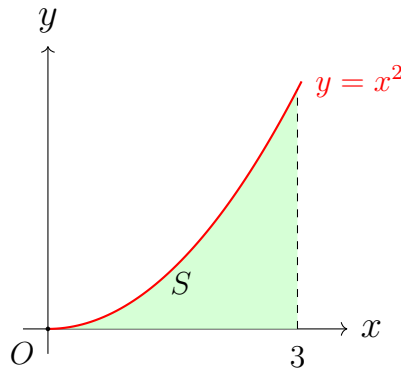
- (A) 1
- (B)  $\frac{\pi}{2}$
- (C)  $\frac{\pi}{2} - 1$
- (D)  $\frac{\pi}{2} + 1$

**Q2.** The value of  $\int_0^{\pi} \sin x \, dx$  is:

- (A) 0
- (B) 1
- (C)  $\pi$
- (D) 2



**Q3.** The area of the region bounded by the curve  $y = x^2$ , the  $x$ -axis, and the line  $x = 3$ , shown shaded below, is:

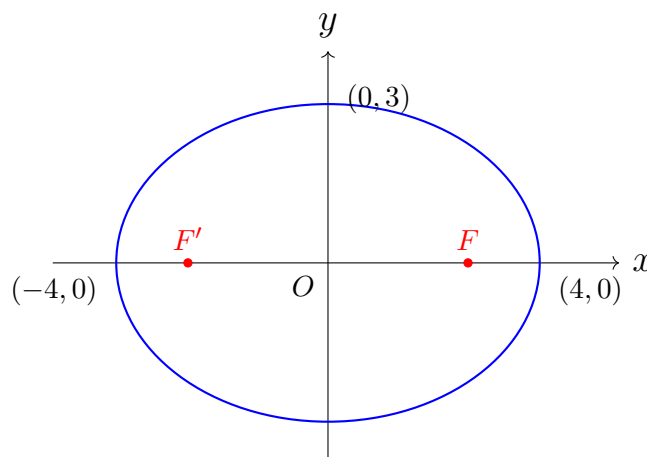


- (A) 9
- (B) 27
- (C)  $\frac{27}{2}$
- (D) 3

**Q4.** The equation of the circle with centre  $(1, 2)$  and radius 3, in general form, is:

- (A)  $x^2 + y^2 + 2x + 4y - 4 = 0$
- (B)  $x^2 + y^2 - 2x - 4y - 4 = 0$
- (C)  $x^2 + y^2 - 2x - 4y + 4 = 0$
- (D)  $x^2 + y^2 - 2x - 4y + 14 = 0$

**Q5.** The eccentricity of the ellipse  $\frac{x^2}{16} + \frac{y^2}{9} = 1$ , sketched below, is:



- (A)  $\frac{3}{4}$
- (B)  $\frac{\sqrt{7}}{3}$
- (C)  $\frac{\sqrt{7}}{4}$
- (D)  $\frac{4}{\sqrt{7}}$

**Q6.** The coordinates of the focus of the parabola  $y^2 = 8x$  are:

- (A) (2, 0)
- (B) (0, 2)
- (C) (-2, 0)
- (D) (4, 0)

**Q7.** If  $A = \begin{pmatrix} 2 & 3 \\ 1 & 4 \end{pmatrix}$ , then  $\det(A)$  equals:

- (A) 11
- (B) -5
- (C) 8
- (D) 5

**Q8.** If  $A = \begin{pmatrix} 3 & 1 \\ 2 & 1 \end{pmatrix}$ , then  $A^{-1}$  equals:

- (A)  $\begin{pmatrix} 1 & 1 \\ 2 & 3 \end{pmatrix}$
- (B)  $\begin{pmatrix} 1 & -1 \\ -2 & 3 \end{pmatrix}$
- (C)  $\begin{pmatrix} 3 & -1 \\ -2 & 1 \end{pmatrix}$
- (D)  $\begin{pmatrix} -1 & 1 \\ 2 & -3 \end{pmatrix}$



**Q9.**  $\lim_{x \rightarrow 0} \frac{1 - \cos x}{x^2}$  equals:

- (A) 0
- (B) 1
- (C)  $\frac{1}{2}$
- (D) 2

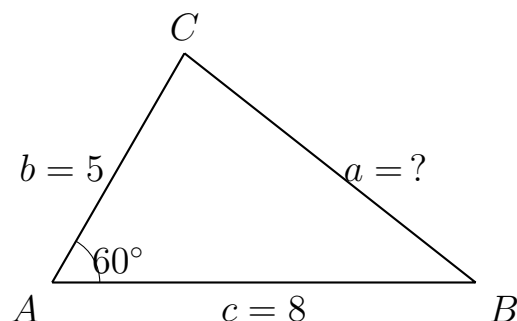
**Q10.** If  $y = x^3 e^x$ , then  $\frac{dy}{dx}$  is:

- (A)  $3x^2 e^x$
- (B)  $x^3 e^x$
- (C)  $x^2 e^x (3 - x)$
- (D)  $x^2 e^x (x + 3)$

**Q11.**  $\cos(A + B) \cdot \cos(A - B)$  equals:

- (A)  $\cos^2 A - \sin^2 B$
- (B)  $\cos^2 A + \sin^2 B$
- (C)  $\sin^2 A - \cos^2 B$
- (D)  $\cos^2 B - \sin^2 A$

**Q12.** In triangle  $ABC$ ,  $\angle A = 60^\circ$ ,  $b = 5$  and  $c = 8$ . The length of side  $a$  is:



- (A)  $\sqrt{129}$
- (B) 7
- (C)  $\sqrt{89}$



(D)  $\sqrt{39}$

**Q13.** Two fair dice are thrown together. The probability that the sum of the numbers shown is 7 is:

(A)  $\frac{1}{12}$

(B)  $\frac{5}{36}$

(C)  $\frac{1}{6}$

(D)  $\frac{7}{36}$

**Q14.** From a group of 5 boys and 4 girls, 3 students are chosen at random. The probability that all three chosen are boys is:

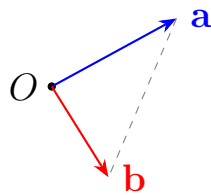
(A)  $\frac{1}{14}$

(B)  $\frac{5}{14}$

(C)  $\frac{10}{21}$

(D)  $\frac{5}{42}$

**Q15.** If  $\mathbf{a} = 3\hat{i} + \hat{j} + 2\hat{k}$  and  $\mathbf{b} = \hat{i} + 2\hat{j} - \hat{k}$ , the value of  $\mathbf{a} \cdot \mathbf{b}$  is:



(A) 7

(B) -3

(C) 1

(D) 3

**Q16.** If  $|\mathbf{a}| = 2$ ,  $|\mathbf{b}| = 5$  and the angle between **a** and **b** is  $30^\circ$ , then  $|\mathbf{a} \times \mathbf{b}|$  equals:



- (A) 5
- (B) 10
- (C)  $5\sqrt{3}$
- (D)  $\frac{5}{2}$

**Q17.** The number of distinct arrangements of the letters of the word **APPLE** is:

- (A) 120
- (B) 60
- (C) 24
- (D) 30

**Q18.** The sum of the first 10 natural numbers  $1 + 2 + 3 + \dots + 10$  is:

- (A) 45
- (B) 100
- (C) 55
- (D) 50

**Q19.** The distance between the points  $(1, 2, 3)$  and  $(4, 6, 3)$  is:

- (A) 5
- (B)  $\sqrt{34}$
- (C) 7
- (D)  $\sqrt{43}$

**Q20.** The general solution of the differential equation  $\frac{dy}{dx} = x$  is:

- (A)  $y = x + C$
- (B)  $y = \frac{x^2}{2} + C$
- (C)  $y = x^2 + C$
- (D)  $y = Cx$



## Detailed Solutions

Q1.

## Solution

**Concept – Integration by Parts:**

$$\int u dv = uv - \int v du. \text{ Choose } u = x, dv = \cos x dx.$$

**Step 1 – Assign  $u$  and  $dv$ :**

$$u = x \Rightarrow du = dx, \quad dv = \cos x dx \Rightarrow v = \sin x$$

**Step 2 – Apply the formula:**

$$\int_0^{\pi/2} x \cos x dx = \left[ x \sin x \right]_0^{\pi/2} - \int_0^{\pi/2} \sin x dx$$

**Step 3 – Evaluate the first term:**

$$\left[ x \sin x \right]_0^{\pi/2} = \frac{\pi}{2} \sin \frac{\pi}{2} - 0 \cdot \sin 0 = \frac{\pi}{2} \cdot 1 = \frac{\pi}{2}$$

**Step 4 – Evaluate the integral:**

$$\int_0^{\pi/2} \sin x dx = \left[ -\cos x \right]_0^{\pi/2} = -\cos \frac{\pi}{2} - (-\cos 0) = -0 + 1 = 1$$

**Step 5 – Combine:**

$$\frac{\pi}{2} - 1$$

**Why other options are wrong:**

- (A) 1: keeping only the subtracted integral.
- (B)  $\frac{\pi}{2}$ : dropping the subtracted integral entirely.
- (D)  $\frac{\pi}{2} + 1$ : sign error in the IBP formula.

**Answer: (C)** [← Go Back to Q1](#)

Q2.

**Solution****Concept – Antiderivative of  $\sin x$ :**

$$\int \sin x \, dx = -\cos x + C$$

**Step 1 – Write the definite integral:**

$$\int_0^{\pi} \sin x \, dx = \left[ -\cos x \right]_0^{\pi}$$

**Step 2 – Substitute the upper limit:**

$$-\cos \pi = -(-1) = 1$$

**Step 3 – Substitute the lower limit:**

$$-\cos 0 = -(1) = -1$$

**Step 4 – Subtract:**

$$1 - (-1) = 2$$

**Why other options are wrong:**

- (A) 0: treating the integrand as odd over a symmetric interval (it is not).
- (B) 1: evaluating only the upper-limit term.
- (C)  $\pi$ : confusing with the length of the interval.

**Answer: (D)** [← Go Back to Q2](#)

Q3.

**Solution****Concept – Area under a curve above the  $x$ -axis:**

$$A = \int_a^b y \, dx$$

**Step 1 – Identify the limits and the function:**The region runs from  $x = 0$  to  $x = 3$  with  $y = x^2$ .

**Step 2 – Set up the integral:**

$$A = \int_0^3 x^2 dx$$

**Step 3 – Integrate:**

$$= \left[ \frac{x^3}{3} \right]_0^3$$

**Step 4 – Evaluate:**

$$= \frac{3^3}{3} - \frac{0^3}{3} = \frac{27}{3} - 0 = 9$$

**Why other options are wrong:**

- (B) 27: forgetting to divide by 3 after integrating.
- (C)  $\frac{27}{2}$ : integrating as if  $y = x$  (using  $x^2/2$ ).
- (D) 3: stopping at  $x = 3$  without integrating.

**Answer: (A)** ← [Go Back to Q3](#)

**Q4.**

### Solution

**Concept – Standard circle equation:**

$(x - h)^2 + (y - k)^2 = r^2$  for centre  $(h, k)$  and radius  $r$ .

**Step 1 – Write the equation with centre  $(1, 2)$ ,  $r = 3$ :**

$$(x - 1)^2 + (y - 2)^2 = 9$$

**Step 2 – Expand  $(x - 1)^2$ :**

$$x^2 - 2x + 1$$

**Step 3 – Expand  $(y - 2)^2$ :**

$$y^2 - 4y + 4$$

**Step 4 – Collect all terms:**

$$x^2 - 2x + 1 + y^2 - 4y + 4 = 9$$

$$x^2 + y^2 - 2x - 4y + 5 = 9$$

**Step 5 – Rearrange:**

$$x^2 + y^2 - 2x - 4y - 4 = 0$$



**Why other options are wrong:**

- (A) has  $+2x + 4y$ : signs of both linear coefficients are wrong.
- (C) has  $+4$ : constant on the right side is not moved correctly.
- (D) has  $+14$ : adding 9 instead of subtracting it.

**Answer: (B)** [← Go Back to Q4](#)

**Q5.**

### Solution

**Concept – Eccentricity of ellipse**  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  **with**  $a > b$ :

$$c^2 = a^2 - b^2, \quad e = \frac{c}{a}$$

**Step 1 – Read off  $a^2$  and  $b^2$ :**

$$a^2 = 16, \quad b^2 = 9$$

**Step 2 – Compute  $c^2$ :**

$$c^2 = 16 - 9 = 7$$

**Step 3 – Compute  $c$ :**

$$c = \sqrt{7}$$

**Step 4 – Compute eccentricity:**

$$e = \frac{c}{a} = \frac{\sqrt{7}}{4}$$

**Why other options are wrong:**

- (A)  $\frac{3}{4}$ : using  $b/a$  instead of  $c/a$ .
- (B)  $\frac{\sqrt{7}}{3}$ : dividing  $c$  by  $b$  instead of  $a$ .
- (D)  $\frac{4}{\sqrt{7}}$ : inverting the ratio  $c/a$ .

**Answer: (C)** [← Go Back to Q5](#)



Q6.

**Solution****Concept – Standard parabola**  $y^2 = 4ax$ :Focus is at  $(a, 0)$  and the axis is the  $x$ -axis.**Step 1 – Match**  $y^2 = 8x$  to  $y^2 = 4ax$ :

$$4a = 8 \Rightarrow a = 2$$

**Step 2 – State the focus:**

$$\text{Focus} = (a, 0) = (2, 0)$$

**Why other options are wrong:**

- (B)  $(0, 2)$ : confusing this parabola with  $x^2 = 4ay$  (vertical axis).
- (C)  $(-2, 0)$ : focus of the leftward parabola  $y^2 = -8x$ .
- (D)  $(4, 0)$ : using  $a = 4$  from  $4a = 8$  incorrectly (taking  $a = 4a/2$  wrong).

**Answer: (A)** [← Go Back to Q6](#)

Q7.

**Solution****Concept –  $2 \times 2$  determinant:**

$$\det \begin{pmatrix} a & b \\ c & d \end{pmatrix} = ad - bc$$

**Step 1 – Identify elements:**

$$a = 2, b = 3, c = 1, d = 4$$

**Step 2 – Compute:**

$$\det(A) = 2 \times 4 - 3 \times 1 = 8 - 3 = 5$$

**Why other options are wrong:**

- (A) 11: adding instead of subtracting  $(8 + 3)$ .
- (B)  $-5$ : reversing the subtraction order  $(bc - ad)$ .
- (C) 8: taking only the main diagonal product.

**Answer: (D)** [← Go Back to Q7](#)

Q8.

**Solution****Concept –  $2 \times 2$  matrix inverse:**

$$\begin{pmatrix} a & b \\ c & d \end{pmatrix}^{-1} = \frac{1}{ad - bc} \begin{pmatrix} d & -b \\ -c & a \end{pmatrix}$$

**Step 1 – Compute  $\det(A)$ :**

$$\det(A) = 3 \times 1 - 1 \times 2 = 3 - 2 = 1$$

**Step 2 – Form the adjugate (swap main diagonal, negate off-diagonal):**

$$\text{adj}(A) = \begin{pmatrix} 1 & -1 \\ -2 & 3 \end{pmatrix}$$

**Step 3 – Divide by  $\det(A) = 1$ :**

$$A^{-1} = \begin{pmatrix} 1 & -1 \\ -2 & 3 \end{pmatrix}$$

**Step 4 – Verify  $A \cdot A^{-1} = I$ :**

$$\begin{pmatrix} 3 & 1 \\ 2 & 1 \end{pmatrix} \begin{pmatrix} 1 & -1 \\ -2 & 3 \end{pmatrix} = \begin{pmatrix} 3 - 2 & -3 + 3 \\ 2 - 2 & -2 + 3 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \checkmark$$

**Why other options are wrong:**

- (A): no sign change on off-diagonal elements.
- (C): main diagonal not swapped (kept 3 and 1 in place).
- (D): all signs reversed.

**Answer: (B)** [← Go Back to Q8](#)

Q9.

**Solution****Concept – Half-angle plus standard limit:**

$$1 - \cos x = 2 \sin^2 \frac{x}{2}, \quad \lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$$

**Step 1 – Rewrite the numerator:**

$$\frac{1 - \cos x}{x^2} = \frac{2 \sin^2 \frac{x}{2}}{x^2}$$

**Step 2 – Write  $x^2 = 4 \left(\frac{x}{2}\right)^2$ :**

$$= \frac{2 \sin^2 \frac{x}{2}}{4 \left(\frac{x}{2}\right)^2} = \frac{1}{2} \cdot \left(\frac{\sin \frac{x}{2}}{\frac{x}{2}}\right)^2$$

**Step 3 – Take the limit as  $x \rightarrow 0$  (so  $\frac{x}{2} \rightarrow 0$ ):**

$$= \frac{1}{2} \cdot (1)^2 = \frac{1}{2}$$

**Why other options are wrong:**

- (A) 0: stopping after noting the numerator  $\rightarrow 0$ , ignoring the rate.
- (B) 1: forgetting the factor  $\frac{1}{2}$ .
- (D) 2: using  $1 - \cos x \approx x^2$  instead of  $\frac{x^2}{2}$ .

**Answer: (C)** [← Go Back to Q9](#)

Q10.

**Solution****Concept – Product Rule:**

$$\frac{d}{dx}(uv) = u'v + uv'$$

**Step 1 – Set  $u = x^3$ ,  $v = e^x$ :**

$$u' = 3x^2, \quad v' = e^x$$

**Step 2 – Apply the product rule:**

$$\frac{dy}{dx} = 3x^2 e^x + x^3 e^x$$



**Step 3 – Factor out  $x^2e^x$ :**

$$= x^2e^x(3 + x) = x^2e^x(x + 3)$$

**Why other options are wrong:**

- (A)  $3x^2e^x$ : differentiating only the  $x^3$  factor.
- (B)  $x^3e^x$ : differentiating only the  $e^x$  factor.
- (C)  $x^2e^x(3 - x)$ : sign error when collecting terms.

**Answer: (D)** ← [Go Back to Q10](#)

**Q11.**

### Solution

**Concept – Difference of squares from compound angles.**

**Step 1 – Expand  $\cos(A + B)$ :**

$$\cos(A + B) = \cos A \cos B - \sin A \sin B$$

**Step 2 – Expand  $\cos(A - B)$ :**

$$\cos(A - B) = \cos A \cos B + \sin A \sin B$$

**Step 3 – Multiply using  $(p - q)(p + q) = p^2 - q^2$ :**

$$\begin{aligned} \cos(A + B) \cdot \cos(A - B) &= (\cos A \cos B)^2 - (\sin A \sin B)^2 \\ &= \cos^2 A \cos^2 B - \sin^2 A \sin^2 B \end{aligned}$$

**Step 4 – Substitute  $\cos^2 B = 1 - \sin^2 B$  and  $\sin^2 A = 1 - \cos^2 A$ :**

$$\begin{aligned} &= \cos^2 A(1 - \sin^2 B) - (1 - \cos^2 A) \sin^2 B \\ &= \cos^2 A - \cos^2 A \sin^2 B - \sin^2 B + \cos^2 A \sin^2 B \\ &= \cos^2 A - \sin^2 B \end{aligned}$$

**Why other options are wrong:**

- (B)  $\cos^2 A + \sin^2 B$ : missing the sign change in the difference of squares.
- (C)  $\sin^2 A - \cos^2 B$ : this is the negative of the correct result.
- (D)  $\cos^2 B - \sin^2 A$ : a valid equivalent rearrangement only by coincidence; here it equals  $\cos(A + B) \cos(A - B)$  written wrongly with  $A, B$  swapped.



**Answer: (A)** ← [Go Back to Q11](#)

Q12.

### Solution

**Concept – Cosine Rule:**

$$a^2 = b^2 + c^2 - 2bc \cos A$$

**Step 1 – Substitute**  $A = 60^\circ$ ,  $b = 5$ ,  $c = 8$ :

$$a^2 = 5^2 + 8^2 - 2(5)(8) \cos 60^\circ$$

**Step 2 – Compute each part:**

$$a^2 = 25 + 64 - 80 \times \frac{1}{2}$$

**Step 3 – Simplify:**

$$a^2 = 89 - 40 = 49$$

**Step 4 – Take positive square root:**

$$a = \sqrt{49} = 7$$

**Why other options are wrong:**

- (A)  $\sqrt{129}$ : using  $+2bc \cos A$  (wrong sign in the rule).
- (C)  $\sqrt{89}$ : omitting the  $-2bc \cos A$  term entirely.
- (D)  $\sqrt{39}$ : using  $80 \cos 60^\circ = 80$  wrongly, or  $\cos 60^\circ = \frac{5}{8}$ .

**Answer: (B)** ← [Go Back to Q12](#)

Q13.

### Solution

**Concept – Classical probability:**

$$P = \frac{\text{favourable outcomes}}{\text{total outcomes}}$$

**Step 1 – Total outcomes for two dice:**

$$6 \times 6 = 36$$



**Step 2 – List the pairs summing to 7:**

$$(1, 6), (2, 5), (3, 4), (4, 3), (5, 2), (6, 1)$$

**Step 3 – Count favourable outcomes:**

$$6$$

**Step 4 – Compute the probability:**

$$P = \frac{6}{36} = \frac{1}{6}$$

**Why other options are wrong:**

- (A)  $\frac{1}{12}$ : counting only 3 ordered pairs.
- (B)  $\frac{5}{36}$ : this is  $P(\text{sum} = 6)$  or  $P(\text{sum} = 8)$ , not 7.
- (D)  $\frac{7}{36}$ : miscounting one extra pair.

**Answer: (C)** ← [Go Back to Q13](#)

**Q14.**

### Solution

**Concept – Classical probability using combinations:**

$$P = \frac{\text{favourable}}{\text{total}}$$

**Step 1 – Total students:  $5 + 4 = 9$ . Total ways to choose 3 from 9:**

$$\binom{9}{3} = \frac{9 \times 8 \times 7}{3 \times 2 \times 1} = 84$$

**Step 2 – Ways to choose 3 boys from 5:**

$$\binom{5}{3} = \frac{5 \times 4 \times 3}{3 \times 2 \times 1} = 10$$

**Step 3 – Compute the probability:**

$$P = \frac{10}{84} = \frac{5}{42}$$

**Why other options are wrong:**



- (A)  $\frac{1}{14}$ : this equals  $\binom{4}{3}/\binom{9}{3} = 4/84$ , the all-girls case.
- (B)  $\frac{5}{14}$ : not reduced correctly; over-counts favourable cases.
- (C)  $\frac{10}{21}$ : dividing 10 by 21 instead of 84.

**Answer: (D)** [← Go Back to Q14](#)

Q15.

### Solution

**Concept – Dot product:**

$$\mathbf{a} \cdot \mathbf{b} = a_1b_1 + a_2b_2 + a_3b_3$$

**Step 1 – Write components:**

$$\mathbf{a} = (3, 1, 2), \quad \mathbf{b} = (1, 2, -1)$$

**Step 2 – Multiply component pairs:**

$$3 \times 1 = 3$$

$$1 \times 2 = 2$$

$$2 \times (-1) = -2$$

**Step 3 – Sum:**

$$\mathbf{a} \cdot \mathbf{b} = 3 + 2 + (-2) = 3$$

**Why other options are wrong:**

- (A) 7: treating all products as positive:  $3 + 2 + 2 = 7$ .
- (B) -3: sign error giving the negative of the correct value.
- (C) 1: arithmetic slip such as  $3 - 2 + 0$ .

**Answer: (D)** [← Go Back to Q15](#)



Q16.

**Solution****Concept – Magnitude of cross product:**

$$|\mathbf{a} \times \mathbf{b}| = |\mathbf{a}||\mathbf{b}| \sin \theta$$

**Step 1 – State given values:**

$$|\mathbf{a}| = 2, \quad |\mathbf{b}| = 5, \quad \theta = 30^\circ$$

**Step 2 – Recall  $\sin 30^\circ$ :**

$$\sin 30^\circ = \frac{1}{2}$$

**Step 3 – Substitute:**

$$|\mathbf{a} \times \mathbf{b}| = 2 \times 5 \times \frac{1}{2} = 10 \times \frac{1}{2} = 5$$

**Why other options are wrong:**

- (B) 10: using  $\sin 30^\circ = 1$  or confusing cross with dot product.
- (C)  $5\sqrt{3}$ : using  $\sin 60^\circ = \frac{\sqrt{3}}{2}$  instead of  $\sin 30^\circ$ .
- (D)  $\frac{5}{2}$ : an extra incorrect halving.

**Answer: (A)** ← [Go Back to Q16](#)

Q17.

**Solution****Concept – Permutations of letters with a repeat:**

$$\text{Number of arrangements} = \frac{n!}{p!}$$

where  $n$  is the total number of letters and  $p!$  accounts for a repeated letter.**Step 1 – Count letters of APPLE:  $A, P, P, L, E$ , so  $n = 5$ .**The letter  $P$  repeats twice.**Step 2 – Compute  $5!$ :**

$$5! = 5 \times 4 \times 3 \times 2 \times 1 = 120$$

**Step 3 – Divide by  $2!$  for the two identical P's:**

$$\frac{120}{2!} = \frac{120}{2} = 60$$



**Why other options are wrong:**

- (A) 120: treating all five letters as distinct ( $5!$ ).
- (C) 24: computing  $4!$ , dropping one letter.
- (D) 30: dividing 120 by 4 instead of 2.

**Answer: (B)** ← [Go Back to Q17](#)

**Q18.**

### Solution

**Concept – Sum of first  $n$  natural numbers:**

$$S_n = \frac{n(n+1)}{2}$$

**Step 1 – Set  $n = 10$ :**

$$S_{10} = \frac{10 \times 11}{2}$$

**Step 2 – Multiply the numerator:**

$$= \frac{110}{2}$$

**Step 3 – Divide:**

$$= 55$$

**Why other options are wrong:**

- (A) 45: summing 1 to 9 only.
- (B) 100: using  $n^2$  ( $10^2$ ) instead of the correct formula.
- (D) 50: using  $\frac{n^2}{2} = \frac{100}{2}$  incorrectly.

**Answer: (C)** ← [Go Back to Q18](#)

**Q19.**

### Solution

**Concept – Distance formula in 3D:**

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$$

**Step 1 – Compute the coordinate differences:**

$$x_2 - x_1 = 4 - 1 = 3$$



$$y_2 - y_1 = 6 - 2 = 4$$

$$z_2 - z_1 = 3 - 3 = 0$$

**Step 2 – Square each difference:**

$$3^2 = 9, \quad 4^2 = 16, \quad 0^2 = 0$$

**Step 3 – Sum the squares:**

$$9 + 16 + 0 = 25$$

**Step 4 – Take the square root:**

$$d = \sqrt{25} = 5$$

**Why other options are wrong:**

- (B)  $\sqrt{34}$ : squaring the wrong differences ( $3^2 + 5^2$ ).
- (C) 7: adding  $3 + 4$  instead of using the formula.
- (D)  $\sqrt{43}$ : an arithmetic slip in summing the squares.

**Answer: (A)** [← Go Back to Q19](#)

**Q20.**

### Solution

**Concept – Direct integration:**

When  $\frac{dy}{dx}$  depends only on  $x$ , integrate both sides with respect to  $x$ .

**Step 1 – Separate the differentials:**

$$dy = x dx$$

**Step 2 – Integrate both sides:**

$$\int dy = \int x dx$$

**Step 3 – Carry out the integration:**

$$y = \frac{x^2}{2} + C$$

**Why other options are wrong:**



- (A)  $y = x + C$ : general solution of  $\frac{dy}{dx} = 1$ , not  $x$ .
- (C)  $y = x^2 + C$ : forgetting the factor  $\frac{1}{2}$  from  $\int x dx$ .
- (D)  $y = Cx$ : general solution of  $\frac{dy}{dx} = \frac{y}{x}$ .

**Answer: (B)** [← Go Back to Q20](#)



**Answer Key**

Q	Ans	Q	Ans	Q	Ans	Q	Ans	Q	Ans
1	C	2	D	3	A	4	B	5	C
6	A	7	D	8	B	9	C	10	D
11	A	12	B	13	C	14	D	15	D
16	A	17	B	18	C	19	A	20	B

