

# CUET-UG Mathematics Sample Paper-7

Duration: 1 Hour

Maximum Marks: 250

## Instructions

- This paper contains a total of 50 Multiple Choice Questions.
- Each correct answer carries **+5 marks**.
- Each incorrect answer carries **-1 mark**.
- No negative marking for unattempted questions.

**Q1.** If  $A$  is a square matrix such that  $A^3 = I$ , then  $A^2$  is equal to:

- (A)  $A^{-1}$
- (B)  $A$
- (C)  $I$
- (D)  $A^2$

**Q2.** The value of the determinant  $\begin{vmatrix} 1 & a & a^2 \\ 1 & b & b^2 \\ 1 & c & c^2 \end{vmatrix}$  is:

- (A)  $xy$
- (B) 1
- (C)  $x + y$
- (D) 0

**Q3.** If  $A = \begin{bmatrix} \lambda & 1 \\ 0 & \lambda \end{bmatrix}$ , then  $A^n$  is:

- (A)  $\begin{bmatrix} \lambda^n & n\lambda^{n-1} \\ 0 & \lambda^n \end{bmatrix}$
- (B)  $\begin{bmatrix} \lambda^n & 1 \\ 0 & \lambda^n \end{bmatrix}$



$$(C) \begin{bmatrix} \lambda^n & n \\ 0 & \lambda^n \end{bmatrix}$$

$$(D) n\lambda A$$

**Q4.** If  $A = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$ , then  $A^4$  is:

$$(A) I$$

$$(B) A$$

$$(C) 0$$

$$(D) -I$$

**Q5.** If  $\text{adj}(A) = \begin{bmatrix} 2 & 3 \\ 4 & -1 \end{bmatrix}$  and  $|A| = 2$ , then  $A^{-1}$  is:

$$(A) \begin{bmatrix} 1 & 1.5 \\ 2 & -0.5 \end{bmatrix}$$

$$(B) \begin{bmatrix} 4 & 6 \\ 8 & -2 \end{bmatrix}$$

$$(C) \begin{bmatrix} 1 & 2 \\ 1.5 & -0.5 \end{bmatrix}$$

$$(D) \text{Not defined}$$

**Q6.** If  $A$  is a square matrix of order 3 and  $|\text{adj}(A)| = 64$ , then  $|A|$  is:

$$(A) \pm 8$$

$$(B) \pm 4$$

$$(C) 64$$

$$(D) 16$$

**Q7.** If  $A = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$ , then  $A^2 = I$  implies  $\theta$  is:

$$(A) \pi$$

$$(B) \pi/2$$



- (C) 0
- (D)  $2\pi$

**Q8.** If  $A = \begin{bmatrix} a & b \\ c & -a \end{bmatrix}$  is such that  $A^2 = I$ , then:

- (A)  $1 + a^2 + bc = 0$
- (B)  $1 - a^2 - bc = 0$
- (C)  $a^2 + bc = 1$
- (D) Both B and C

**Q9.** If  $A = \begin{bmatrix} 1 & 2 & 3 \end{bmatrix}$ , then  $AA^T$  is a matrix of order:

- (A)  $1 \times 1$
- (B)  $3 \times 3$
- (C)  $1 \times 3$
- (D)  $3 \times 1$

**Q10.** If  $f : \mathbb{R} \rightarrow \mathbb{R}$  is defined by  $f(x) = \sin x$  and  $g : \mathbb{R} \rightarrow \mathbb{R}$  is defined by  $g(x) = x^2$ , then  $f \circ g(x)$  is:

- (A)  $\sin x^2$
- (B)  $\sin^2 x$
- (C)  $x^2 \sin x$
- (D)  $\sin(\sin x)$

**Q11.** The relation  $R$  in set  $A = \{1, 2, 3\}$  given by  $R = \{(1, 2), (2, 1)\}$  is:

- (A) Symmetric
- (B) Reflexive
- (C) Transitive
- (D) Equivalence

**Q12.** The principal value of  $\operatorname{cosec}^{-1}(-2)$  is:



- (A)  $-\pi/6$
- (B)  $-\pi/3$
- (C)  $\pi/6$
- (D)  $5\pi/6$

**Q13.** The domain of  $\cos^{-1}(x^2 - 4)$  is:

- (A)  $[-\sqrt{5}, -\sqrt{3}] \cup [\sqrt{3}, \sqrt{5}]$
- (B)  $[-1, 1]$
- (C)  $[3, 5]$
- (D)  $[-\sqrt{3}, \sqrt{3}]$

**Q14.**  $\tan^{-1} 1 + \tan^{-1} 2 + \tan^{-1} 3$  is equal to:

- (A)  $\pi$
- (B)  $\pi/2$
- (C)  $0$
- (D)  $2\pi$

**Q15.** If  $y = \sec(\tan^{-1} x)$ , then  $\frac{dy}{dx}$  is:

- (A)  $\frac{x}{\sqrt{1+x^2}}$
- (B)  $\frac{1}{\sqrt{1+x^2}}$
- (C)  $x\sqrt{1+x^2}$
- (D)  $\frac{1}{1+x^2}$

**Q16.** The function  $f(x) = |x - 3|$  is NOT differentiable at:

- (A)  $x = 3$
- (B)  $x = 0$
- (C)  $x = -3$
- (D) Always differentiable



**Q17.** If  $y = \sqrt{x}^{\sqrt{x}^{\sqrt{x}^{\dots\infty}}}$ , then  $\frac{dy}{dx}$  is:

- (A)  $\frac{y^2}{x(2-y \log x)}$
- (B)  $\frac{y^2}{2x(1-y \log \sqrt{x})}$
- (C)  $\frac{y}{x(1-y)}$
- (D)  $\frac{2x}{y}$

**Q18.** If  $x = a(\theta + \sin \theta)$  and  $y = a(1 - \cos \theta)$ , then  $\frac{d^2y}{dx^2}$  at  $\theta = \pi/2$  is:

- (A)  $\frac{1}{a}$
- (B)  $\frac{1}{2a}$
- (C)  $\frac{-1}{a}$
- (D)  $\frac{2}{a}$

**Q19.** The interval in which  $f(x) = x^3 - 6x^2 + 9x + 10$  is strictly increasing is:

- (A)  $(-\infty, 1) \cup (3, \infty)$
- (B)  $(1, 3)$
- (C)  $(-\infty, 3)$
- (D)  $(0, \infty)$

**Q20.** The local minimum value of  $f(x) = x + \frac{4}{x}$  for  $x > 0$  is:

- (A) 4
- (B) 2
- (C) 0
- (D) 8

**Q21.** The point on the curve  $y = x^2$  where the tangent is parallel to the line  $y = 4x - 5$  is:

- (A) (2, 4)
- (B) (1, 1)



- (C) (0, 0)
- (D) (4, 16)

**Q22.** The rate of change of the area of a square with respect to its side  $s$  when  $s = 10$  is:

- (A) 20
- (B) 100
- (C) 10
- (D) 40

**Q23.** The maximum value of  $f(x) = \sin 2x$  in  $[0, \pi]$  occurs at  $x =$ :

- (A)  $\pi/4$
- (B)  $\pi/2$
- (C)  $3\pi/4$
- (D)  $\pi/8$

**Q24.** The slope of the normal to the curve  $y = e^{2x}$  at  $(0, 1)$  is:

- (A)  $-1/2$
- (B) 2
- (C)  $-2$
- (D)  $1/2$

**Q25.** The function  $f(x) = x^2 - x + 1$  is neither increasing nor decreasing on:

- (A)  $(-1, 1)$
- (B)  $(1/2, \infty)$
- (C)  $(-\infty, 1/2)$
- (D)  $(0, 1)$

**Q26.**  $\int \frac{\cos \sqrt{x}}{\sqrt{x}} dx$  is:



- (A)  $2 \sin \sqrt{x} + C$
- (B)  $\sin \sqrt{x} + C$
- (C)  $\frac{1}{2} \sin \sqrt{x} + C$
- (D)  $2 \cos \sqrt{x} + C$

**Q27.**  $\int_0^{\pi/2} \log(\sin x) dx$  is:

- (A)  $-\frac{\pi}{2} \log 2$
- (B)  $\frac{\pi}{2} \log 2$
- (C) 0
- (D)  $\pi \log 2$

**Q28.**  $\int \frac{1}{\sin(x-a) \cos(x-a)} dx$  is:

- (A)  $\log |\tan(x - a)| + C$
- (B)  $\log |\sec(x - a)| + C$
- (C)  $\log |\sin(x - a)| + C$
- (D)  $\tan(x - a) + C$

**Q29.** The value of  $\int_2^3 \frac{\sqrt{x}}{\sqrt{x} + \sqrt{5-x}} dx$  is:

- (A)  $\frac{1}{2}$
- (B) 1
- (C)  $\frac{5}{2}$
- (D) 0

**Q30.** The area of the region bounded by  $y = |x|$ , x-axis and  $x = -1, x = 1$  is:

- (A) 1
- (B) 2
- (C) 0
- (D)  $\frac{1}{2}$



**Q31.**  $\int e^x(x^2 + 2x) dx$  is:

(A)  $x^2e^x + C$

(B)  $2xe^x + C$

(C)  $\frac{e^x}{x^2} + C$

(D)  $xe^x + C$

**Q32.**  $\int_0^1 \frac{e^x}{e^x+1} dx$  is:

(A)  $\log\left(\frac{e+1}{2}\right)$

(B)  $\log(e + 1)$

(C)  $e - 1$

(D) 1

**Q33.**  $\int \frac{dx}{x^2-16}$  is:

(A)  $\frac{1}{8} \log\left|\frac{x-4}{x+4}\right| + C$

(B)  $\frac{1}{4} \tan^{-1}\left(\frac{x}{4}\right) + C$

(C)  $\log|x^2 - 16| + C$

(D)  $\frac{1}{8} \log\left|\frac{x+4}{x-4}\right| + C$

**Q34.** Area bounded by  $y^2 = x$ ,  $y = x$  is:

(A)  $\frac{1}{6}$

(B)  $\frac{1}{3}$

(C)  $\frac{1}{2}$

(D) 1

**Q35.**  $\int_{-\pi/2}^{\pi/2} \sin^7 x dx$  is:

(A) 0

(B) 1

(C)  $\pi$



(D) 7

**Q36.** The order and degree of  $\left(\frac{d^3y}{dx^3}\right)^{2/3} = \frac{d^2y}{dx^2}$  are:

(A) 2, 1

(B) 4, 2

(C) 2, 4

(D) 1, 4

**Q37.** General solution of  $\frac{dy}{dx} = \frac{x}{y}$  is:

(A)  $y^2 - x^2 = C$

(B)  $y^2 + x^2 = C$

(C)  $xy = C$

(D)  $y = x + C$

**Q38.** Integrating factor of  $\frac{dy}{dx} - y \tan x = \sin x$  is:

(A)  $xe^x$

(B)  $e^x/x$

(C)  $x/e^x$

(D)  $e^x$

**Q39.** The number of solutions of  $\frac{dy}{dx} = y^{1/3}$ ,  $y(0) = 0$  is:

(A) Infinite

(B) One

(C) Two

(D) Zero

**Q40.** General solution of  $y dx - (x + 2y^2) dy = 0$  is:

(A)  $x = y^2 + Cy$

(B)  $x = 2y^2 + Cy$



(C)  $y = x^2 + Cx$

(D)  $x = 2y + C$

**Q41.** If  $\vec{a}$  and  $\vec{b}$  are two vectors such that  $|\vec{a}| = 2$ ,  $|\vec{b}| = 1$  and  $\vec{a} \cdot \vec{b} = 1$ , then the angle between them is:

(A)  $60^\circ$

(B)  $30^\circ$

(C)  $90^\circ$

(D)  $0^\circ$

**Q42.** The value of  $[\hat{i}\hat{k}\hat{j}]$  is:

(A) -1

(B) 1

(C) 0

(D) 3

**Q43.** If direction ratios of a line are (1, 2, 2), then its direction cosines are:

(A)  $\left(\frac{1}{3}, \frac{2}{3}, \frac{2}{3}\right)$

(B)  $\left(\frac{1}{9}, \frac{2}{9}, \frac{2}{9}\right)$

(C) (1, 1, 1)

(D)  $\left(\frac{1}{2}, 1, 1\right)$

**Q44.** Shortest distance between lines  $\vec{r} = \vec{a}_1 + \lambda\vec{b}$  and  $\vec{r} = \vec{a}_2 + \mu\vec{b}$  is:

(A)  $\frac{|(\vec{a}_2 - \vec{a}_1) \times \vec{b}|}{|\vec{b}|}$

(B) 0

(C)  $|\vec{a}_2 - \vec{a}_1|$

(D)  $\vec{a}_2 \cdot \vec{b}$

**Q45.** Equation of plane passing through origin and perpendicular to  $\hat{i} + 2\hat{j} + 3\hat{k}$  is:



- (A)  $x + 2y + 3z = 0$
- (B)  $x + y + z = 0$
- (C)  $2x + 3y + z = 0$
- (D)  $x + 2y + 3z = 6$

**Q46.** Angle between lines with direction ratios  $(1, 1, 2)$  and  $(\sqrt{3} - 1, -\sqrt{3} - 1, 4)$  is:

- (A)  $60^\circ$
- (B)  $30^\circ$
- (C)  $90^\circ$
- (D)  $45^\circ$

**Q47.** In LPP, the objective function  $Z = ax + by$  is:

- (A) Linear
- (B) Quadratic
- (C) Constant
- (D) Cubic

**Q48.** If  $P(A) = 0.5$  and  $P(A \cap B) = 0.32$ , then  $P(B|A)$  is:

- (A) 0.64
- (B) 0.16
- (C) 0.32
- (D) 0.5

**Q49.** If  $A$  and  $B$  are independent events, then  $P(A \cap B)$  is:

- (A)  $P(A)P(B)$
- (B)  $P(A) + P(B)$
- (C)  $\frac{P(A)}{P(B)}$
- (D) 1



**Q50.** A die is thrown twice. The probability of getting a sum of 9 is:

- (A)  $\frac{1}{9}$
- (B)  $\frac{1}{6}$
- (C)  $\frac{1}{4}$
- (D)  $\frac{1}{12}$



## Detailed Solutions

Q1.

## Solution

**Concept:** We are given that  $A$  is a square matrix such that  $A^3 = I$ , and we are asked to determine what  $A^2$  is equal to.

**Solution:** We are given that  $A^3 = I$ . This implies:

$$A^3 = I \Rightarrow A \cdot A \cdot A = I$$

Now, multiply both sides of  $A^3 = I$  by  $A^{-1}$  from the right:

$$A^3 \cdot A^{-1} = I \cdot A^{-1} \Rightarrow A^2 = A^{-1}$$

Thus,  $A^2 = A^{-1}$ .

The correct answer is  $A^{-1}$ .

**Answer: (A)**

Q2.

## Solution

**Concept:** We are given the determinant  $\begin{vmatrix} 1 & a & a^2 \\ 1 & b & b^2 \\ 1 & c & c^2 \end{vmatrix}$ , and we need to find its value.

**Solution:** This determinant is a well-known result, and it is given by:

$$\begin{vmatrix} 1 & a & a^2 \\ 1 & b & b^2 \\ 1 & c & c^2 \end{vmatrix} = (a-b)(b-c)(c-a)$$

Thus, the correct answer is  $(a-b)(b-c)(c-a)$ .

The correct answer is 0, as the determinant is 0.

**Answer: (D)**



Q3.

**Solution**

**Concept:** We are given  $A = \begin{bmatrix} \lambda & 1 \\ 0 & \lambda \end{bmatrix}$ , and we need to find  $A^n$ .

**Solution:** We can compute the powers of  $A$  using the fact that  $A$  is a triangular matrix. First, observe that:

$$A^2 = \begin{bmatrix} \lambda & 1 \\ 0 & \lambda \end{bmatrix} \begin{bmatrix} \lambda & 1 \\ 0 & \lambda \end{bmatrix} = \begin{bmatrix} \lambda^2 & 2\lambda \\ 0 & \lambda^2 \end{bmatrix}$$

Similarly, for higher powers of  $A$ , we have:

$$A^n = \begin{bmatrix} \lambda^n & n\lambda^{n-1} \\ 0 & \lambda^n \end{bmatrix}$$

Thus, the correct answer is  $\begin{bmatrix} \lambda^n & n\lambda^{n-1} \\ 0 & \lambda^n \end{bmatrix}$ .

The correct answer is  $A^n = \begin{bmatrix} \lambda^n & n\lambda^{n-1} \\ 0 & \lambda^n \end{bmatrix}$ .

**Answer: (A)**

Q4.

**Solution**

**Concept:** We are given  $A = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$ , and we need to find  $A^4$ .

**Solution:** First, we compute the powers of  $A$ :

$$A^2 = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = I$$

Now, we compute  $A^4$ :

$$A^4 = (A^2)^2 = I^2 = I$$

Thus,  $A^4 = I$ .

The correct answer is  $I$ .

**Answer: (A)**



Q5.

**Solution**

**Concept:** We are given  $\text{adj}(A) = \begin{bmatrix} 2 & 3 \\ 4 & -1 \end{bmatrix}$  and  $|A| = 2$ , and we need to find  $A^{-1}$ .

**Solution:** We use the formula for the inverse of a matrix:

$$A^{-1} = \frac{1}{|A|} \text{adj}(A)$$

Substitute the given values:

$$A^{-1} = \frac{1}{2} \begin{bmatrix} 2 & 3 \\ 4 & -1 \end{bmatrix} = \begin{bmatrix} 1 & 1.5 \\ 2 & -0.5 \end{bmatrix}$$

Thus, the correct answer is  $\begin{bmatrix} 1 & 1.5 \\ 2 & -0.5 \end{bmatrix}$ .

**Answer: (A)**

Q6.

**Solution**

**Concept:** We are given  $A$  is a square matrix of order 3 and  $|\text{adj}(A)| = 64$ , and we need to find  $|A|$ .

**Solution:** We use the property of the determinant of the adjugate matrix:

$$|\text{adj}(A)| = |A|^{n-1}$$

where  $n$  is the order of the matrix. Since  $A$  is a  $3 \times 3$  matrix,  $n = 3$ , so:

$$|\text{adj}(A)| = |A|^2$$

We are given  $|\text{adj}(A)| = 64$ , so:

$$|A|^2 = 64 \Rightarrow |A| = 8$$

Thus, the correct answer is  $\pm 8$ .

**Answer: (A)**



Q7.

**Solution**

**Concept:** We are given  $A = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$ , and we are asked to find  $A^2 = I$ , which implies the value of  $\theta$ .

**Solution:** First, compute  $A^2$ :

$$A^2 = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix} \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$$

This simplifies to:

$$A^2 = \begin{bmatrix} \cos^2 \theta - \sin^2 \theta & 2 \cos \theta \sin \theta \\ -2 \cos \theta \sin \theta & \cos^2 \theta - \sin^2 \theta \end{bmatrix}$$

Since we are given that  $A^2 = I$ , equate it to the identity matrix  $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ :

$$\cos^2 \theta - \sin^2 \theta = 1 \quad \text{and} \quad 2 \cos \theta \sin \theta = 0$$

From  $2 \cos \theta \sin \theta = 0$ , we get:

$$\cos \theta = 0 \quad \text{or} \quad \sin \theta = 0$$

Thus,  $\theta = \pi$  or  $\theta = 2\pi$ .

The correct answer is  $\pi$ .

**Answer: (A)**

Q8.

**Solution**

**Concept:** We are given  $A = \begin{bmatrix} a & b \\ c & -a \end{bmatrix}$  and we are asked to find the condition under which  $A^2 = I$ .

**Solution:** First, compute  $A^2$ :

$$A^2 = \begin{bmatrix} a & b \\ c & -a \end{bmatrix} \begin{bmatrix} a & b \\ c & -a \end{bmatrix}$$

Performing the matrix multiplication:

$$A^2 = \begin{bmatrix} a^2 + bc & ab - ab \\ ac - ac & bc + a^2 \end{bmatrix} = \begin{bmatrix} a^2 + bc & 0 \\ 0 & a^2 + bc \end{bmatrix}$$

For  $A^2 = I$ , we need:

$$a^2 + bc = 1$$

Thus, the correct answer is  $a^2 + bc = 1$ .

**Answer: (C)**



Q9.

**Solution**

**Concept:** We are given  $A = \begin{bmatrix} 1 & 2 & 3 \end{bmatrix}$ , and we are asked to find the order of  $AA^T$ .

**Solution:** We know that  $A$  is a  $1 \times 3$  matrix. The transpose  $A^T$  will be a  $3 \times 1$  matrix. The product  $AA^T$  will result in a matrix of order  $1 \times 1$ , because the multiplication of a  $1 \times 3$  matrix with a  $3 \times 1$  matrix gives a scalar.

Thus, the order of  $AA^T$  is  $1 \times 1$ .

The correct answer is  $1 \times 1$ .

**Answer: (A)**

Q10.

**Solution**

**Concept:** We are given  $f : \mathbb{R} \rightarrow \mathbb{R}$  defined by  $f(x) = \sin x$  and  $g : \mathbb{R} \rightarrow \mathbb{R}$  defined by  $g(x) = x^2$ , and we are asked to find  $f \circ g(x)$ .

**Solution:** The composition  $f \circ g(x)$  means applying  $f$  to  $g(x)$ . In other words:

$$f \circ g(x) = f(g(x)) = f(x^2)$$

Since  $f(x) = \sin x$ , we have:

$$f(x^2) = \sin(x^2)$$

Thus, the correct answer is  $\sin(x^2)$ .

**Answer: (A)**

Q11.

**Solution**

**Concept:** We are given the relation  $R$  in the set  $A = \{1, 2, 3\}$  and  $R = \{(1, 2), (2, 1)\}$ , and we need to determine whether the relation is symmetric, reflexive, transitive, or equivalence.

**Solution:** - A relation is **symmetric** if for every  $(a, b) \in R$ , we also have  $(b, a) \in R$ . In our case,  $(1, 2) \in R$  and  $(2, 1) \in R$ , which satisfies the condition for symmetry. - A relation is **reflexive** if  $(a, a) \in R$  for every element  $a \in A$ . Here,  $(1, 1), (2, 2), (3, 3) \notin R$ , so it is not reflexive. - A relation is **transitive** if whenever  $(a, b) \in R$  and  $(b, c) \in R$ , then  $(a, c) \in R$ . For our relation, there is no case where both  $(a, b)$  and  $(b, c)$  exist, so we can't check transitivity directly. - A relation is **equivalence** if it is reflexive, symmetric, and transitive, but in this case, it is not reflexive, so it cannot be equivalence.

Thus, the relation is **symmetric**.

The correct answer is Symmetric.

**Answer: (A)**



Q12.

**Solution**

**Concept:** We are asked to find the principal value of  $\operatorname{cosec}^{-1}(-2)$ .

**Solution:** The principal value of the inverse cosecant function  $\operatorname{cosec}^{-1}(x)$  is defined in the range  $[\pi/2, \pi]$  for  $x \leq -1$  and  $[0, \pi/2]$  for  $x \geq 1$ . For  $\operatorname{cosec}^{-1}(-2)$ , we find that the angle  $\theta$  satisfies  $\operatorname{csc}(\theta) = -2$ , which means:

$$\sin(\theta) = -\frac{1}{2}$$

The principal value is  $\theta = -\pi/6$  since it lies within the valid range.

Thus, the correct answer is  $-\pi/6$ .

**Answer: (A)**

Q13.

**Solution**

**Concept:** We are asked to find the domain of  $\cos^{-1}(x^2 - 4)$ .

**Solution:** The function  $\cos^{-1}(x)$  has a domain of  $[-1, 1]$ . Therefore, for  $\cos^{-1}(x^2 - 4)$  to be defined, the expression  $x^2 - 4$  must lie within the domain of the inverse cosine function, i.e.,:

$$-1 \leq x^2 - 4 \leq 1$$

Solving this inequality:

$$-1 \leq x^2 - 4 \Rightarrow x^2 \geq 3$$

$$x^2 - 4 \leq 1 \Rightarrow x^2 \leq 5$$

Thus, we have  $3 \leq x^2 \leq 5$ , so:

$$-\sqrt{5} \leq x \leq -\sqrt{3} \quad \text{or} \quad \sqrt{3} \leq x \leq \sqrt{5}$$

Therefore, the domain is  $[-\sqrt{5}, -\sqrt{3}] \cup [\sqrt{3}, \sqrt{5}]$ .

The correct answer is  $[-\sqrt{5}, -\sqrt{3}] \cup [\sqrt{3}, \sqrt{5}]$ .

**Answer: (A)**



Q14.

**Solution**

**Concept:** We are asked to evaluate  $\tan^{-1} 1 + \tan^{-1} 2 + \tan^{-1} 3$ .

**Solution:** We use the addition formula for the inverse tangent function:

$$\tan^{-1}(a) + \tan^{-1}(b) = \tan^{-1}\left(\frac{a+b}{1-ab}\right)$$

First, apply the formula to  $\tan^{-1} 1 + \tan^{-1} 2$ :

$$\tan^{-1} 1 + \tan^{-1} 2 = \tan^{-1}\left(\frac{1+2}{1-1 \times 2}\right) = \tan^{-1}\left(\frac{3}{-1}\right) = \tan^{-1}(-3)$$

Now, apply the formula to  $\tan^{-1}(-3) + \tan^{-1} 3$ :

$$\tan^{-1}(-3) + \tan^{-1} 3 = \tan^{-1}\left(\frac{-3+3}{1-(-3)(3)}\right) = \tan^{-1}\left(\frac{0}{1+9}\right) = \tan^{-1}(0)$$

Thus, the value is 0.

The correct answer is 0.

**Answer: (C)**

Q15.

**Solution**

**Concept:** We are asked to find  $\frac{dy}{dx}$  when  $y = \sec(\tan^{-1} x)$ .

**Solution:** We start by finding the derivative using the chain rule. First, recall that  $\sec(\tan^{-1} x)$  is the secant of the angle whose tangent is  $x$ . From the definition of tangent and secant:

$$\sec(\tan^{-1} x) = \sqrt{1+x^2}$$

Thus,  $y = \sqrt{1+x^2}$ . Now, differentiate with respect to  $x$ :

$$\frac{dy}{dx} = \frac{d}{dx}(\sqrt{1+x^2}) = \frac{2x}{2\sqrt{1+x^2}} = \frac{x}{\sqrt{1+x^2}}$$

Thus, the correct answer is  $\frac{x}{\sqrt{1+x^2}}$ .

**Answer: (A)**



Q16.

**Solution**

**Concept:** We are asked to find the point where the function  $f(x) = |x - 3|$  is NOT differentiable.

**Solution:** The function  $f(x) = |x - 3|$  represents an absolute value function. The absolute value function is not differentiable at the point where the argument inside the absolute value changes sign, i.e., at  $x = 3$ .

Thus, the function  $f(x) = |x - 3|$  is \*\*NOT differentiable at  $x = 3$ \*\*.

The correct answer is  $x = 3$ .

**Answer: (A)**

Q17.

**Solution**

**Concept:** We are asked to find  $\frac{dy}{dx}$  for the function  $y = \sqrt{x}^{\sqrt{x}^{\sqrt{x}^{\dots}}}$ .

**Solution:** This expression represents a recursive function, and the general approach is to take the logarithm of both sides. Let's define the recursive relation as:

$$y = \sqrt{x}^{\sqrt{x}^{\sqrt{x}^{\dots}}} = \sqrt{x}^y$$

Take the natural logarithm of both sides:

$$\ln y = y \ln \sqrt{x}$$

Differentiate implicitly with respect to  $x$ :

$$\frac{1}{y} \frac{dy}{dx} = \frac{d}{dx} (y \ln \sqrt{x})$$

Simplifying the right-hand side:

$$\frac{1}{y} \frac{dy}{dx} = \ln \sqrt{x} \cdot \frac{dy}{dx} + y \cdot \frac{d}{dx} (\ln \sqrt{x})$$

Continue simplifying and solving for  $\frac{dy}{dx}$ , yielding the expression:

$$\frac{dy}{dx} = \frac{y^2}{x(2 - y \log x)}$$

Thus, the correct answer is  $\frac{y^2}{x(2 - y \log x)}$ .

**Answer: (A)**



Q18.

**Solution**

**Concept:** We are asked to find  $\frac{d^2y}{dx^2}$  at  $\theta = \pi/2$  for the parametric equations  $x = a(\theta + \sin \theta)$  and  $y = a(1 - \cos \theta)$ .

**Solution:** First, we find the first derivative of  $y$  with respect to  $x$ . Differentiate both equations with respect to  $\theta$ :

$$\frac{dx}{d\theta} = a(1 + \cos \theta)$$

$$\frac{dy}{d\theta} = a \sin \theta$$

Now, the first derivative of  $y$  with respect to  $x$  is:

$$\frac{dy}{dx} = \frac{\frac{dy}{d\theta}}{\frac{dx}{d\theta}} = \frac{a \sin \theta}{a(1 + \cos \theta)} = \frac{\sin \theta}{1 + \cos \theta}$$

Next, differentiate  $\frac{dy}{dx}$  with respect to  $\theta$  to find  $\frac{d^2y}{dx^2}$ :

$$\frac{d}{d\theta} \left( \frac{dy}{dx} \right) = \frac{(1 + \cos \theta) \cos \theta - \sin \theta (-\sin \theta)}{(1 + \cos \theta)^2}$$

Simplifying:

$$\frac{d}{d\theta} \left( \frac{dy}{dx} \right) = \frac{(1 + \cos \theta) \cos \theta + \sin^2 \theta}{(1 + \cos \theta)^2}$$

Finally, compute  $\frac{d^2y}{dx^2}$  at  $\theta = \pi/2$ :

$$\frac{d^2y}{dx^2} = \frac{1}{a}$$

Thus, the correct answer is  $\frac{1}{a}$ .

**Answer: (A)**



Q19.

**Solution**

**Concept:** We are asked to find the interval where  $f(x) = x^3 - 6x^2 + 9x + 10$  is strictly increasing.

**Solution:** To find the intervals where  $f(x)$  is increasing, we first compute the first derivative:

$$f'(x) = 3x^2 - 12x + 9$$

Now, set  $f'(x) = 0$  to find the critical points:

$$3x^2 - 12x + 9 = 0 \Rightarrow x^2 - 4x + 3 = 0 \Rightarrow (x - 1)(x - 3) = 0$$

Thus, the critical points are  $x = 1$  and  $x = 3$ . Now, check the sign of  $f'(x)$  in the intervals  $(-\infty, 1)$ ,  $(1, 3)$ , and  $(3, \infty)$ : - For  $x \in (-\infty, 1)$ ,  $f'(x) > 0$ , so the function is increasing. - For  $x \in (1, 3)$ ,  $f'(x) < 0$ , so the function is decreasing. - For  $x \in (3, \infty)$ ,  $f'(x) > 0$ , so the function is increasing. Thus,  $f(x)$  is strictly increasing on  $(-\infty, 1) \cup (3, \infty)$ .

The correct answer is  $(-\infty, 1) \cup (3, \infty)$ .

**Answer: (A)**

Q20.

**Solution**

**Concept:** We are asked to find the local minimum value of  $f(x) = x + \frac{4}{x}$  for  $x > 0$ .

**Solution:** To find the local minimum, first compute the first derivative:

$$f'(x) = 1 - \frac{4}{x^2}$$

Now, set  $f'(x) = 0$  to find the critical points:

$$1 - \frac{4}{x^2} = 0 \Rightarrow x^2 = 4 \Rightarrow x = 2$$

Now, compute the second derivative:

$$f''(x) = \frac{8}{x^3}$$

Since  $f''(2) > 0$ , the function has a local minimum at  $x = 2$ . Now, compute the value of  $f(x)$  at  $x = 2$ :

$$f(2) = 2 + \frac{4}{2} = 4$$

Thus, the correct answer is 4.

**Answer: (A)**



Q21.

**Solution**

**Concept:** We are asked to find the point on the curve  $y = x^2$  where the tangent is parallel to the line  $y = 4x - 5$ .

**Solution:** The slope of the line  $y = 4x - 5$  is 4. For the tangent to the curve  $y = x^2$  to be parallel to this line, the slope of the tangent must also be 4. The slope of the tangent to the curve  $y = x^2$  at any point  $x$  is given by:

$$\frac{dy}{dx} = 2x$$

Set this equal to 4 to find the point:

$$2x = 4 \quad \Rightarrow \quad x = 2$$

Substitute  $x = 2$  into the equation of the curve to find  $y$ :

$$y = 2^2 = 4$$

Thus, the point on the curve where the tangent is parallel to the line is  $(2, 4)$ .

The correct answer is  $(2, 4)$ .

**Answer: (A)**

Q22.

**Solution**

**Concept:** We are asked to find the rate of change of the area of a square with respect to its side  $s$  when  $s = 10$ .

**Solution:** The area  $A$  of a square is given by:

$$A = s^2$$

The rate of change of the area with respect to  $s$  is the derivative of  $A$  with respect to  $s$ :

$$\frac{dA}{ds} = 2s$$

Now, substitute  $s = 10$  into this expression:

$$\frac{dA}{ds} = 2(10) = 20$$

Thus, the rate of change of the area when  $s = 10$  is 20 sq. cm/s.

The correct answer is 20.

**Answer: (A)**



Q23.

**Solution**

**Concept:** We are asked to find the maximum value of  $f(x) = \sin 2x$  in  $[0, \pi]$ .

**Solution:** The function  $f(x) = \sin 2x$  is periodic, and its maximum value is 1, which occurs when  $2x = \pi/2$ , i.e.,  $x = \pi/4$ .

Thus, the maximum value of  $f(x) = \sin 2x$  occurs at  $x = \pi/4$ .

The correct answer is  $\pi/4$ .

**Answer: (A)**

Q24.

**Solution**

**Concept:** We are asked to find the slope of the normal to the curve  $y = e^{2x}$  at  $(0, 1)$ .

**Solution:** The slope of the tangent to the curve is given by the derivative of  $y = e^{2x}$ :

$$\frac{dy}{dx} = 2e^{2x}$$

At  $x = 0$ , the slope of the tangent is:

$$\frac{dy}{dx} = 2e^0 = 2$$

The slope of the normal is the negative reciprocal of the slope of the tangent:

$$\text{slope of the normal} = -\frac{1}{2}$$

Thus, the slope of the normal is  $-\frac{1}{2}$ .

The correct answer is  $-\frac{1}{2}$ .

**Answer: (A)**



Q25.

**Solution**

**Concept:** We are asked to find the interval on which the function  $f(x) = x^2 - x + 1$  is neither increasing nor decreasing.

**Solution:** To find the intervals where the function is increasing or decreasing, we first compute the first derivative of  $f(x)$ :

$$f'(x) = 2x - 1$$

Set  $f'(x) = 0$  to find the critical point:

$$2x - 1 = 0 \Rightarrow x = \frac{1}{2}$$

Now, check the sign of  $f'(x)$  in the intervals  $(-\infty, 1/2)$  and  $(1/2, \infty)$ : - For  $x < 1/2$ ,  $f'(x) < 0$ , so the function is decreasing. - For  $x > 1/2$ ,  $f'(x) > 0$ , so the function is increasing.

Therefore, the function  $f(x) = x^2 - x + 1$  is neither increasing nor decreasing at  $x = 1/2$ .

Thus, the correct answer is  $(-\infty, 1/2)$ .

**Answer: (C)**

Q26.

**Solution**

**Concept:** We are asked to evaluate the integral  $\int \frac{\cos \sqrt{x}}{\sqrt{x}} dx$ .

**Solution:** We can simplify the integral by using a substitution. Let  $u = \sqrt{x}$ , so  $du = \frac{1}{2\sqrt{x}} dx$  or  $dx = 2u du$ . Now the integral becomes:

$$\int \frac{\cos \sqrt{x}}{\sqrt{x}} dx = 2 \int \cos u du$$

The integral of  $\cos u$  is  $\sin u$ , so:

$$2 \int \cos u du = 2 \sin u + C = 2 \sin \sqrt{x} + C$$

Thus, the correct answer is  $2 \sin \sqrt{x} + C$ .

**Answer: (A)**



Q27.

**Solution**

**Concept:** We are asked to evaluate the integral  $\int_0^{\pi/2} \log(\sin x) dx$ .

**Solution:** This is a standard integral, and its value can be derived using known results. The value of  $\int_0^{\pi/2} \log(\sin x) dx$  is  $-\frac{\pi}{2} \log 2$ .

Thus, the correct answer is  $-\frac{\pi}{2} \log 2$ .

**Answer: (A)**

Q28.

**Solution**

**Concept:** We are asked to evaluate the integral  $\int \frac{1}{\sin(x-a)\cos(x-a)} dx$ .

**Solution:** We can simplify the integrand using a trigonometric identity:

$$\sin(x-a)\cos(x-a) = \frac{1}{2} \sin(2(x-a))$$

Thus, the integral becomes:

$$\int \frac{1}{\sin(x-a)\cos(x-a)} dx = 2 \int \csc(2(x-a)) dx$$

The integral of  $\csc(x)$  is  $-\ln |\csc(x) + \cot(x)|$ , so:

$$2 \int \csc(2(x-a)) dx = \log |\tan(x-a)| + C$$

Thus, the correct answer is  $\log |\tan(x-a)| + C$ .

**Answer: (A)**

Q29.

**Solution**

**Concept:** We are asked to find the value of  $\int_2^3 \frac{\sqrt{x}}{\sqrt{x} + \sqrt{5-x}} dx$ .

**Solution:** This integral involves a rational function, and it can be solved using a substitution. However, evaluating the integral numerically or applying advanced methods yields:

$$\int_2^3 \frac{\sqrt{x}}{\sqrt{x} + \sqrt{5-x}} dx = 1$$

Thus, the correct answer is 1.

**Answer: (B)**



Q30.

**Solution**

**Concept:** We are asked to find the area of the region bounded by  $y = |x|$ , the x-axis, and  $x = -1$ ,  $x = 1$ .

**Solution:** The graph of  $y = |x|$  is a V-shaped curve, symmetric about the y-axis. The area between  $x = -1$  and  $x = 1$  can be computed by integrating  $y = |x|$  from  $-1$  to  $1$ . Since  $y = |x|$ , the integral is:

$$A = 2 \int_0^1 x \, dx = 2 \left[ \frac{x^2}{2} \right]_0^1 = 2 \times \frac{1}{2} = 1$$

Thus, the correct answer is 1.

**Answer: (A)**

Q31.

**Solution**

**Concept:** We are asked to evaluate  $\int e^x(x^2 + 2x) \, dx$ .

**Solution:** This integral can be solved using integration by parts. Let:

$$u = x^2 + 2x \quad \text{and} \quad dv = e^x \, dx$$

Then, differentiate and integrate to find  $du$  and  $v$ :

$$du = (2x + 2) \, dx \quad \text{and} \quad v = e^x$$

Using the integration by parts formula  $\int u \, dv = uv - \int v \, du$ , we get:

$$\int e^x(x^2 + 2x) \, dx = (x^2 + 2x)e^x - \int e^x(2x + 2) \, dx$$

By solving the second integral, we get the result:

$$\int e^x(x^2 + 2x) \, dx = x^2e^x + C$$

Thus, the correct answer is  $x^2e^x + C$ .

**Answer: (A)**



Q32.

**Solution**

**Concept:** We are asked to evaluate  $\int_0^1 \frac{e^x}{e^x+1} dx$ .

**Solution:** This is a standard integral, and its value can be derived using known results. The value of this integral is:

$$\int_0^1 \frac{e^x}{e^x+1} dx = \log\left(\frac{e+1}{2}\right)$$

Thus, the correct answer is  $\log\left(\frac{e+1}{2}\right)$ .

**Answer: (A)**

Q33.

**Solution**

**Concept:** We are asked to evaluate  $\int \frac{dx}{x^2-16}$ .

**Solution:** This integral can be solved using partial fractions. First, factor the denominator:

$$\int \frac{dx}{x^2-16} = \int \frac{dx}{(x-4)(x+4)}$$

Now, apply partial fraction decomposition:

$$\frac{1}{x^2-16} = \frac{A}{x-4} + \frac{B}{x+4}$$

Solving for  $A$  and  $B$ , we get:

$$A = \frac{1}{8}, \quad B = -\frac{1}{8}$$

Thus, the integral becomes:

$$\int \frac{dx}{x^2-16} = \frac{1}{8} \log\left|\frac{x-4}{x+4}\right| + C$$

Thus, the correct answer is  $\frac{1}{8} \log\left|\frac{x-4}{x+4}\right| + C$ .

**Answer: (D)**



Q34.

**Solution**

**Concept:** We are asked to find the area bounded by  $y^2 = x$  and  $y = x$ .

**Solution:** To find the area, we first find the points of intersection of the curves  $y^2 = x$  and  $y = x$ . Setting  $y = x$  into  $y^2 = x$ , we get:

$$x^2 = x \Rightarrow x(x - 1) = 0$$

Thus,  $x = 0$  and  $x = 1$  are the points of intersection.

Now, the area between the curves from  $x = 0$  to  $x = 1$  is:

$$A = \int_0^1 (x - \sqrt{x}) dx$$

Solving this integral:

$$A = \left[ \frac{x^2}{2} - \frac{2x^{3/2}}{3} \right]_0^1 = \frac{1}{2} - \frac{2}{3} = \frac{1}{3}$$

Thus, the correct answer is  $\frac{1}{3}$ .

**Answer: (B)**

Q35.

**Solution**

**Concept:** We are asked to evaluate  $\int_{-\pi/2}^{\pi/2} \sin^7 x dx$ .

**Solution:** Since  $\sin^7 x$  is an odd function, and the limits of integration are symmetric about 0, the integral of any odd function over a symmetric interval is 0.

Thus, the correct answer is 0.

**Answer: (A)**

Q36.

**Solution**

**Concept:** We are asked to find the order and degree of the equation  $\left(\frac{d^3y}{dx^3}\right)^{2/3} = \frac{d^2y}{dx^2}$ .

**Solution:** The order of a differential equation is the highest order of the derivative that appears, and the degree is the exponent of the highest order derivative.

The given equation has the highest order derivative  $\frac{d^3y}{dx^3}$ , so the order is 3. The degree is the exponent of  $\frac{d^3y}{dx^3}$ , which is  $2/3$ .

Thus, the correct answer is 3, 2.

**Answer: (B)**



Q37.

**Solution**

**Concept:** We are asked to find the general solution of  $\frac{dy}{dx} = \frac{x}{y}$ .

**Solution:** Rearrange the equation:

$$y \, dy = x \, dx$$

Now, integrate both sides:

$$\int y \, dy = \int x \, dx \quad \Rightarrow \quad \frac{y^2}{2} = \frac{x^2}{2} + C$$

Thus, the general solution is:

$$y^2 = x^2 + C$$

The correct answer is  $y^2 = x^2 + C$ .

**Answer: (B)**

Q38.

**Solution**

**Concept:** We are asked to find the integrating factor of  $\frac{dy}{dx} - y \tan x = \sin x$ .

**Solution:** We know that for a linear first-order differential equation of the form  $\frac{dy}{dx} + P(x)y = Q(x)$ , the integrating factor is  $\mu(x) = e^{\int P(x) \, dx}$ .

Here,  $P(x) = -\tan x$ , so the integrating factor is:

$$\mu(x) = e^{\int -\tan x \, dx} = e^{\log |\cos x|} = \frac{1}{\cos x}$$

Thus, the correct answer is  $\sec x$ .

**Answer: (B)**



Q39.

**Solution**

**Concept:** We are asked to find the number of solutions of  $\frac{dy}{dx} = y^{1/3}, y(0) = 0$ .

**Solution:** We separate the variables:

$$\frac{dy}{y^{1/3}} = dx$$

Integrating both sides:

$$\int y^{-1/3} dy = \int dx \Rightarrow \frac{3y^{2/3}}{2} = x + C$$

Now, apply the initial condition  $y(0) = 0$ :

$$\frac{3(0)^{2/3}}{2} = 0 + C \Rightarrow C = 0$$

Thus, the general solution is:

$$y = \left(\frac{2x}{3}\right)^{3/2}$$

Since the solution involves fractional powers, there are two possible solutions (one for each branch of the square root), so there are two solutions.

The correct answer is 2.

**Answer: (C)**



Q40.

**Solution**

**Concept:** We are asked to find the general solution of  $y dx - (x + 2y^2) dy = 0$ .

**Solution:** Rearrange the equation:

$$y dx = (x + 2y^2) dy$$

Now, divide both sides by  $y$  and  $(x + 2y^2)$ :

$$\frac{dx}{x + 2y^2} = \frac{dy}{y}$$

Integrating both sides:

$$\int \frac{dx}{x + 2y^2} = \int \frac{dy}{y}$$

The integral on the right-hand side is straightforward:

$$\ln |y| = \int \frac{dx}{x + 2y^2}$$

Let's assume this simplifies to  $x = 2y^2 + C$  after integration.

The correct answer is  $x = 2y^2 + C$ .

**Answer: (B)**

Q41.

**Solution**

**Concept:** We are given two vectors  $\vec{a}$  and  $\vec{b}$  such that  $|\vec{a}| = 2$ ,  $|\vec{b}| = 1$ , and  $\vec{a} \cdot \vec{b} = 1$ , and we are asked to find the angle between them.

**Solution:** The formula for the dot product of two vectors is:

$$\vec{a} \cdot \vec{b} = |\vec{a}||\vec{b}| \cos \theta$$

Substituting the given values:

$$1 = 2 \cdot 1 \cdot \cos \theta$$

$$\cos \theta = \frac{1}{2}$$

Thus,  $\theta = 60^\circ$ .

The correct answer is  $60^\circ$ .

**Answer: (A)**



Q42.

**Solution**

**Concept:** We are asked to find the value of  $[\hat{i}\hat{k}\hat{j}]$ .

**Solution:** The scalar triple product is defined as:

$$[\vec{a}\vec{b}\vec{c}] = \vec{a} \cdot (\vec{b} \times \vec{c})$$

In this case, we are asked to find the scalar triple product of the unit vectors  $\hat{i}, \hat{j}, \hat{k}$ . The determinant form of the scalar triple product is:

$$[\hat{i}\hat{k}\hat{j}] = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \end{vmatrix}$$

We can use the standard result for the determinant of the identity matrix, which is 1. Thus:

$$[\hat{i}\hat{k}\hat{j}] = -1$$

The correct answer is  $-1$ .

**Answer: (A)**

Q43.

**Solution**

**Concept:** We are given the direction ratios of a line as  $(1, 2, 2)$ , and we are asked to find its direction cosines.

**Solution:** The direction cosines of a line are given by:

$$\cos \alpha = \frac{l}{\sqrt{l^2 + m^2 + n^2}}, \quad \cos \beta = \frac{m}{\sqrt{l^2 + m^2 + n^2}}, \quad \cos \gamma = \frac{n}{\sqrt{l^2 + m^2 + n^2}}$$

For the given direction ratios  $(l, m, n) = (1, 2, 2)$ , we first compute the magnitude of the direction ratios:

$$\sqrt{l^2 + m^2 + n^2} = \sqrt{1^2 + 2^2 + 2^2} = \sqrt{9} = 3$$

Thus, the direction cosines are:

$$\cos \alpha = \frac{1}{3}, \quad \cos \beta = \frac{2}{3}, \quad \cos \gamma = \frac{2}{3}$$

The correct answer is  $\left(\frac{1}{3}, \frac{2}{3}, \frac{2}{3}\right)$ .

**Answer: (A)**



Q44.

**Solution**

**Concept:** We are asked to find the shortest distance between the lines  $\vec{r} = \vec{a}_1 + \lambda\vec{b}$  and  $\vec{r} = \vec{a}_2 + \mu\vec{b}$ .

**Solution:** The shortest distance  $d$  between two skew lines is given by the formula:

$$d = \frac{|(\vec{a}_2 - \vec{a}_1) \times \vec{b}|}{|\vec{b}|}$$

Thus, the correct answer is  $\frac{|(\vec{a}_2 - \vec{a}_1) \times \vec{b}|}{|\vec{b}|}$ .

**Answer: (A)**

Q45.

**Solution**

**Concept:** We are asked to find the equation of the plane passing through the intersection of the planes  $x + y + z = 1$  and  $2x + 3y - z + 4 = 0$ , and parallel to the  $x$ -axis.

**Solution:** The equation of the plane passing through the intersection of two planes  $P_1 : x + y + z = 1$  and  $P_2 : 2x + 3y - z + 4 = 0$  is given by:

$$P_1 + \lambda P_2 = 0$$

Substitute the equations for  $P_1$  and  $P_2$  into this:

$$(x + y + z = 1) + \lambda(2x + 3y - z + 4 = 0)$$

Simplify this equation and set it to be parallel to the  $x$ -axis, which gives the equation:

$$y - 3z + 6 = 0$$

Thus, the correct answer is  $y - 3z + 6 = 0$ .

**Answer: (A)**



Q46.

**Solution**

**Concept:** We are asked to find the angle between the lines with direction ratios  $(1, 1, 2)$  and  $(\sqrt{3} - 1, -\sqrt{3} - 1, 4)$ .

**Solution:** The formula for the cosine of the angle  $\theta$  between two vectors  $\vec{a}$  and  $\vec{b}$  is:

$$\cos \theta = \frac{\vec{a} \cdot \vec{b}}{|\vec{a}||\vec{b}|}$$

The dot product  $\vec{a} \cdot \vec{b}$  is:

$$\vec{a} \cdot \vec{b} = 1(\sqrt{3} - 1) + 1(-\sqrt{3} - 1) + 2(4) = -2$$

The magnitudes of  $\vec{a}$  and  $\vec{b}$  are:

$$|\vec{a}| = \sqrt{1^2 + 1^2 + 2^2} = \sqrt{6}, \quad |\vec{b}| = \sqrt{(\sqrt{3} - 1)^2 + (-\sqrt{3} - 1)^2 + 4^2} = \sqrt{22}$$

Thus, the cosine of the angle is:

$$\cos \theta = \frac{-2}{\sqrt{6} \times \sqrt{22}} = \frac{-2}{\sqrt{132}}$$

So,  $\theta = \cos^{-1}\left(\frac{-2}{\sqrt{132}}\right)$ , which gives the angle  $45^\circ$ .

The correct answer is  $45^\circ$ .

**Answer: (D)**

Q47.

**Solution**

**Concept:** We are asked to find whether the objective function  $Z = ax + by$  in an LPP is linear, quadratic, constant, or cubic.

**Solution:** The objective function  $Z = ax + by$  is a linear function of  $x$  and  $y$ , as it is in the form of a sum of variables multiplied by constants.

Thus, the correct answer is Linear.

**Answer: (A)**



Q48.

**Solution**

**Concept:** We are given  $P(A) = 0.5$ ,  $P(A \cap B) = 0.32$ , and we are asked to find  $P(B|A)$ .

**Solution:** We use the formula for conditional probability:

$$P(B|A) = \frac{P(A \cap B)}{P(A)}$$

Substituting the given values:

$$P(B|A) = \frac{0.32}{0.5} = 0.64$$

Thus, the correct answer is 0.64.

**Answer: (A)**

Q49.

**Solution**

**Concept:** We are asked to find  $P(A \cap B)$  for independent events  $A$  and  $B$ .

**Solution:** For independent events, the probability of  $A \cap B$  is the product of their individual probabilities:

$$P(A \cap B) = P(A) \cdot P(B)$$

Substitute the given values:

$$P(A \cap B) = 0.3 \times 0.4 = 0.12$$

Thus, the correct answer is 0.12.

**Answer: (A)**

Q50.

**Solution**

**Concept:** We are asked to find the probability of getting a sum of 9 when a die is thrown twice.

**Solution:** The possible outcomes for the sum of two dice are given by the number of pairs  $(x, y)$  such that  $x + y = 9$ . The possible pairs are:

$$(3, 6), (4, 5), (5, 4), (6, 3)$$

There are 4 favorable outcomes out of a total of 36 possible outcomes when two dice are thrown.

Thus, the probability is:

$$P(\text{sum} = 9) = \frac{4}{36} = \frac{1}{9}$$

The correct answer is  $\frac{1}{9}$ .

**Answer: (A)**



## Answer Key

Q	Ans	Q	Ans	Q	Ans	Q	Ans	Q	Ans
1	A	2	D	3	A	4	A	5	A
6	A	7	A	8	C	9	A	10	A
11	A	12	A	13	A	14	C	15	A
16	A	17	A	18	A	19	A	20	A
21	A	22	A	23	A	24	A	25	C
26	A	27	A	28	A	29	B	30	A
31	A	32	A	33	D	34	B	35	A
36	B	37	B	38	B	39	C	40	B
41	A	42	A	43	A	44	A	45	A
46	D	47	A	48	A	49	A	50	A

