

MEMORY BASED QUESTIONS JEE-MAIN EXAMINATION – JANUARY 2026

(HELD ON FRIDAY 23rd JANUARY 2026)

TIME : 3:00 PM TO 6:00 PM

MATHEMATICS

TEST PAPER WITH SOLUTION

1. If $\sum_{k=1}^n a_k = \alpha n^2 + \beta n$ & $a_{10} = 59$, $a_6 = 7a_1$, then find

$\alpha + \beta$:

- (1) 5 (2) 10
(3) 8 (4) 3

Ans. (1)

Sol. $\therefore S_n = \alpha n^2 + \beta n$

$$\therefore a_n = S_n - S_{n-1} = \alpha(n^2 - (n-1)^2) + \beta(1) \\ = (2n-1)\alpha + \beta$$

$$\therefore a_{10} = 59 \Rightarrow 19\alpha + \beta = 59 \quad \dots(1)$$

$$a_1 = \alpha + \beta$$

$$a_6 = 11\alpha + \beta$$

$$\therefore a_6 = 7a_1$$

$$11\alpha + \beta = 7\alpha + 7\beta$$

$$4\alpha = 6\beta$$

$$2\alpha = 3\beta \quad \dots(2)$$

From (1) & (2)

$$19\alpha + \frac{2\alpha}{3} = 59$$

$$\boxed{\alpha = 3 \Rightarrow \beta = 2}$$

$$\therefore \boxed{\alpha + \beta = 5}$$

2. The minimum value of

$$\cos^2\theta + 6\sin\theta\cos\theta + 3\sin^2\theta + 3 \text{ is :}$$

- (1) -1 (2) 1
(3) $5 + \sqrt{10}$ (4) $5 - \sqrt{10}$

Ans. (4)

Sol. $3(2\sin\theta\cos\theta) + 2\sin^2\theta + (\cos^2\theta + \sin^2\theta) + 3$

$$= 3\sin 2\theta + (1 - \cos 2\theta) + 4$$

$$= 5 + (3\sin 2\theta - \cos 2\theta)$$

$$\text{So, minimum value} = 5 - \sqrt{9+1}$$

$$= 5 - \sqrt{10}$$

3. If matrices A & B are such that $A = \begin{bmatrix} 0 & -2 & 3 \\ -2 & 0 & 1 \\ -1 & 1 & 0 \end{bmatrix}$,

$B(I - A) = (I + A)$, then find B.

$$(1) B = \begin{bmatrix} -1 & 2/3 & 2/3 \\ -2 & 5/3 & -10/3 \\ -2 & 2 & -3 \end{bmatrix}$$

$$(2) B = \begin{bmatrix} -1 & 1/3 & 1/3 \\ -2 & 5/3 & -10/3 \\ -2 & 2 & -3 \end{bmatrix}$$

$$(3) B = \begin{bmatrix} -1 & 0 & 2/3 \\ 0 & 5/3 & -10/3 \\ 2 & 2 & -3 \end{bmatrix}$$

$$(4) B = \begin{bmatrix} -1 & 2/3 & 2/3 \\ -2/3 & 1 & 5/3 \\ -2 & 2 & -3 \end{bmatrix}$$

Ans. (1)

$$\text{Sol. } I - A = \begin{bmatrix} 1 & 2 & -3 \\ 2 & 1 & -1 \\ 1 & -1 & 1 \end{bmatrix}, I + A = \begin{bmatrix} 1 & -2 & 3 \\ -2 & 1 & 1 \\ -1 & 1 & 1 \end{bmatrix}$$

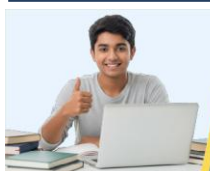
$$|I - A| = 1(0) - 2(3) - 3(-3) \\ = -6 + 9 = 3$$

$$(I - A)^{-1} = \frac{1}{3} \begin{bmatrix} 0 & 1 & 1 \\ -3 & 4 & -5 \\ -3 & 3 & -3 \end{bmatrix}$$

$$B = (I + A)(I - A)^{-1}$$

$$B = \frac{1}{3} \begin{bmatrix} 1 & -2 & 3 \\ -2 & 1 & 1 \\ -1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 0 & 1 & 1 \\ -3 & 4 & -5 \\ -3 & 3 & -3 \end{bmatrix}$$

$$B = \frac{1}{3} \begin{bmatrix} -3 & 2 & 2 \\ -6 & 5 & -10 \\ -6 & 6 & -9 \end{bmatrix}$$



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$$B = \begin{bmatrix} -1 & 2/3 & 2/3 \\ -2 & 5/3 & -10/3 \\ -2 & 2 & -3 \end{bmatrix}$$

4. If $\cot \theta = -\frac{1}{2\sqrt{2}}$ where $\theta \in \left(\frac{3\pi}{2}, 2\pi\right)$ then value of

$$\sin\left(\frac{15\theta}{2}\right) (\sin 8\theta + \cos 8\theta) + \cos\left(\frac{15\theta}{2}\right) (\cos 8\theta - \sin 8\theta)$$

is :

$$(1) \frac{\sqrt{2}+1}{\sqrt{3}} \quad (2) -\left(\frac{\sqrt{2}+1}{\sqrt{3}}\right)$$

$$(3) \frac{\sqrt{2}-1}{\sqrt{3}} \quad (4) -\left(\frac{\sqrt{2}-1}{\sqrt{3}}\right)$$

Ans. (2)

Sol. $\cos\left(8\theta - \frac{15\theta}{2}\right) + \sin\left(\frac{15\theta}{2} - 8\theta\right)$

$$\cos\frac{\theta}{2} - \sin\frac{\theta}{2} = -\sqrt{1 - \sin\theta}$$

$$= -\sqrt{1 + \frac{2\sqrt{2}}{3}}$$

$$= -\sqrt{\frac{3+2\sqrt{2}}{3}} = -\left(\frac{\sqrt{2}+1}{\sqrt{3}}\right)$$

5. Sum of solutions of the equation

$$\log_{x+3}(6x^2 + 28x + 30) = 5 - 2 \log_{6x+10}(x^2 + 6x + 9),$$

are :

$$(1) 0 \quad (2) 1$$

$$(3) 2 \quad (4) 3$$

Ans. (1)

Sol. $\log_{x+3}[(x+3)(6x+10)] = 5 - 2 \log_{6x+10}(x+3)^2$

$$1 + \log_{x+3}(6x+10) = 5 - 4 \log_{6x+10}(x+3)$$

$$\text{Let } \log_{6x+10}(x+3) = t$$

$$1 + \frac{1}{t} = 5 - 4t$$

$$t + 1 = 5t - 4t^2 \Rightarrow 4t^2 - 4t + 1 = 0$$

$$\Rightarrow (2t-1)^2 = 0 \Rightarrow t = \frac{1}{2}$$

$$\therefore \log_{6x+10}(x+3) = \frac{1}{2} \Rightarrow x+3 = (6x+10)^{1/2}$$

$$\Rightarrow x^2 + 6x + 9 = 6x + 10$$

$$\Rightarrow x = 1, -1$$

So, sum of solution = 0

6. If PQ is a chord perpendicular to the transverse axis of $\frac{x^2}{4} - \frac{y^2}{b^2} = 1$ of eccentricity $\sqrt{3}$ such that

ΔOPQ is equilateral Δ (where O is the origin), then area of ΔOPQ is :

$$(1) \frac{4}{5}\sqrt{3} \quad (2) \frac{2}{5}\sqrt{3}$$

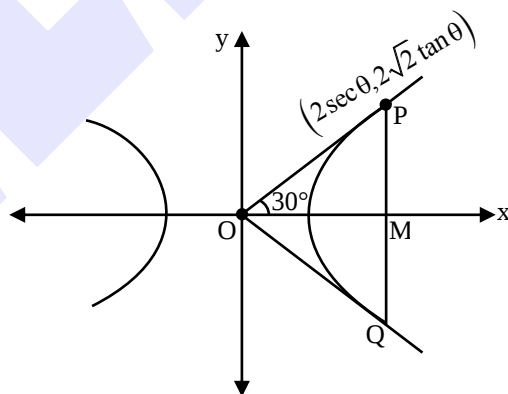
$$(3) \frac{8}{5}\sqrt{3} \quad (4) \frac{16\sqrt{3}}{5}$$

Ans. (3)

Sol. $e = \sqrt{1 + \frac{b^2}{4}} = \sqrt{3}$

$$\Rightarrow b = 8$$

$$\therefore \text{Hyperbola } \frac{x^2}{4} - \frac{y^2}{8} = 1$$

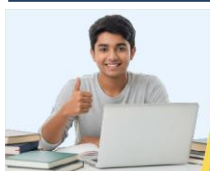


$$\frac{PM}{OM} = \tan 30^\circ$$

$$\Rightarrow \frac{2\sqrt{2} \tan \theta}{2 \sec \theta} = \frac{1}{\sqrt{3}} \Rightarrow \sin \theta = \frac{1}{\sqrt{6}}$$

$$\text{Area} = 2 \times \frac{1}{2} \times OM \times MP$$

$$= 2 \sec \theta \times 2\sqrt{2} \tan \theta$$



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$$= 4\sqrt{2} \frac{\sin \theta}{\cos^2 \theta} = 4\sqrt{2} \times \frac{1}{\sqrt{6} \times \left(1 - \frac{1}{6}\right)} = \frac{8\sqrt{3}}{5}$$

7. If $\vec{a}, \vec{b}, \vec{c}$ are three vectors such that $\vec{a} \times \vec{b} = 2(\vec{a} \times \vec{c})$,
 $|\vec{a}|=1, |\vec{b}|=4, |\vec{c}|=2$ and angle between $\vec{b}$ & $\vec{c}$ is
 60° , then find $|\vec{a} \cdot \vec{c}|$:

- (1) 4 (2) 1
 (3) 2 (4) $\frac{1}{2}$

Ans. (2)

Sol. $\vec{a} \times \vec{b} - 2(\vec{a} \times \vec{c}) = 0$

$$\vec{a} \times (\vec{b} - 2\vec{c}) = 0 \Rightarrow \vec{b} - 2\vec{c} = \lambda \vec{a} \quad \dots(1)$$

$$|\lambda \vec{a}|^2 = |\vec{b} - 2\vec{c}|^2 \Rightarrow \lambda^2 |\vec{a}|^2 = b^2 + 4c^2 - 4\vec{b} \cdot \vec{c}$$

$$\lambda^2 = 16 + 16 - 4 \cdot 4 \cdot 2 \cdot \frac{1}{2}$$

$$\lambda^2 = 16$$

$$\lambda = \pm 4$$

$$\therefore \vec{b} - 2\vec{c} = \pm 4\vec{a}$$

$$\text{Dot with } \vec{c} \Rightarrow \vec{b} \cdot \vec{c} - 2|\vec{c}|^2 = \pm 4(\vec{a} \cdot \vec{c})$$

$$4 \cdot 2 \cdot \frac{1}{2} - 2 \cdot 4 = \pm 4(\vec{a} \cdot \vec{c})$$

$$|\vec{a} \cdot \vec{c}| = 1$$

8. The system of linear equations

$$x + y + z = 6$$

$$2x + 5y + az = 36$$

$$x + 2y + 3z = b$$

- (1) Infinitely many solutions for $a = 8$ & $b = 16$
 (2) Unique solution for $a = 8$ & $b = 16$
 (3) Unique solution for $a = 8$ & $b = 14$
 (4) Infinitely many solutions for $a = 8$ & $b = 14$

Ans. (4)

Sol. If $D = \begin{vmatrix} 1 & 1 & 1 \\ 2 & 5 & a \\ 1 & 2 & 3 \end{vmatrix} = 0 \Rightarrow a = 8$

$$\text{If } D_1 = \begin{vmatrix} 6 & 1 & 1 \\ 36 & 5 & a \\ b & 2 & 3 \end{vmatrix} = 0 \Rightarrow ab - 5b - 12a + 54 = 0$$

$$\text{If } D_2 = \begin{vmatrix} 1 & 6 & 1 \\ 2 & 36 & a \\ 1 & b & 3 \end{vmatrix} = 0 \Rightarrow ab - 6a - 2b - 36 = 0$$

$$\text{If } D_3 = \begin{vmatrix} 1 & 1 & 6 \\ 2 & 5 & 36 \\ 1 & 2 & b \end{vmatrix} = 0 \Rightarrow b = 14$$

For $a = 8$ & $b = 14 \Rightarrow D_1$ & D_2 are also zero

For $a = 8$ & $b = 14 \Rightarrow D = D_1 = D_2 = D_3 = 0$
 $\Rightarrow$ infinitely many solutions.

9. Number of ways of distributing 16 identical oranges among 4 persons such that each one gets atleast one oranges is

- (1) 435 (2) 455
 (3) 470 (4) 489

Ans. (2)

Sol. $x_1 + x_2 + x_3 + x_4 = 16$

Number of positive integral solution
 $= {}^{15}C_3 = 455$

10. $\int_0^x t^2 \sin(x-t) dt = x^2$, then sum of values of x

where $x \in [0, 100]$

- (1) 300π (2) 272π
 (3) 200π (4) 240π

Ans. (4)

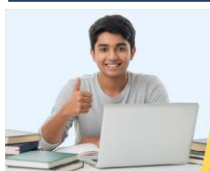
Sol. $\int_0^x (x-t)^2 \sin t dt = x^2$

$$\int_0^x (x^2 - 2xt + t^2) \sin t dt = x^2$$

$$x^2 (-\cos t)_0^x - 2x \int_0^x t \sin t dt + \int_0^x t^2 \sin t dt = x^2$$

$$-x^2 (\cos x - 1) - 2x (-t \cos t + \sin t)_0^x + (t^2 (-\cos t))_0^x + \int_0^x 2t \cos t dt = x^2$$

$$-x^2 \cos x + x^2 - 2x (-x \cos x + \sin x) - x^2 \cos x + 2(t \sin t + \cos t)_0^x = x^2$$



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$$-x^2 \cos x + x^2 + 2x^2 \cos x - 2x \sin x - x^2 \cos x + 2(x \sin x + \cos x - 1) = x^2$$

$$x^2 + 2 \cos x - 2 = x^2$$

$$\cos x = 1$$

$$x = 2m\pi, m \in \mathbb{I}$$

$$0 + 2\pi + 4\pi + \dots + 30\pi$$

$$= 2\pi(1 + 2 + \dots + 15)$$

$$= 2\pi \cdot \frac{15 \cdot 16}{2} = 240\pi$$

11. If $y = f(x)$ satisfies the differential equation $(x^2 - 4)y' - 2xy + 2x(4 - x^2)^2 = 0$ and $f(3) = 15$, then find local maximum value of $f(x)$

- (1) 16 (2) 20
(3) 25 (4) 30

Ans. (1)

Sol.
$$\frac{(x^2 - 4) \frac{dy}{dx} - 2xy}{(4 - x^2)^2} = -2x$$

$$\frac{d}{dx} \left(\frac{y}{x^2 - 4} \right) = -2x$$

$$\therefore \frac{y}{x^2 - 4} = -x^2 + C$$

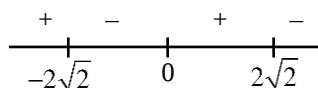
$$\{(3, 15) \Rightarrow \frac{15}{5} = -9 + C \Rightarrow C = 12\}$$

$$\Rightarrow \frac{y}{x^2 - 4} = 12 - x^2$$

$$\Rightarrow y = (x^2 - 4)(12 - x^2)$$

$$y' = (x^2 - 4)(-2x) + (12 - x^2) \cdot 2x$$

$$= -4x(x - 2\sqrt{2})(x + 2\sqrt{2})$$



Local maximum value of

$$f(x) = f(\pm 2\sqrt{2})$$

$$= (8 - 4)(12 - 8) = 16$$

12. Let $A = \{1, 2, 3, \dots, 9\} : x R y$, if $|x - y|$ is multiple of 3.

S_1 : Number of elements in R is 36

S_2 : R is equivalence relation.

- (1) S_1 & S_2 both correct
(2) S_1 & S_2 is correct, but S_2 not correct
(3) S_2 is correct, but S_1 is not correct
(4) S_1 & S_2 both incorrect

Ans. (3)

Sol. Number of numbers of form $3n \Rightarrow 3$

Number of numbers of form $3n + 1 \Rightarrow 3$

Number of numbers of form $3n + 2 \Rightarrow 3$

Number of ordered pairs $(x, y) = 3(3 \times 3) = 27$

S_1 false

$$\Rightarrow x R y \Leftrightarrow y R x$$

$$\Rightarrow (x - y) = 3\lambda, (y - z) = 3\mu$$

$$\Rightarrow (x - z) = 3(\lambda + \mu)$$

R is reflexive, symmetric & transitive

S_2 is true

Ans. S_1 is false but S_2 is true

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13. $f(x) = \begin{cases} \frac{a|x| + 2x^2 - 2\sin|x|\cos|x|}{x} & ; x \neq 0 \\ b & ; x = 0 \end{cases}$

If $f(x)$ is continuous then value of $a + b$ is equal to

- (1) 2 (2) 3
(3) 4 (4) 5

Ans. (1)

Sol. $\lim_{x \rightarrow 0} \left(\frac{a|x| + 2x^2 - 2\sin|x|\cos|x|}{x} \right)$

$f(0^+) = a - 2$

$f(0^-) = -a + 2$

for continuity

$a - 2 = -a + 2 = b \Rightarrow a = 2 \text{ \& } b = 0$

so $a + b = 2$

14. Let sets $A : \{x : |x - 3| - 3 \leq 1\}, x \in \mathbb{Z}$.

set $B : \left\{ x : x \in \mathbb{R} (x \neq 1, 2) \frac{(x-2)(x-4)}{(x-1)} \log_e |x-2| = 0 \right\}$

then number of onto functions from $A \rightarrow B$.

- (1) 61 (2) 62
(3) 63 (4) 64

Ans. (2)

Sol. $A : |x - 3| - 3 \leq 1$

$\Rightarrow -1 \leq |x - 3| - 3 \leq 1$

$2 \leq |x - 3| \leq 4$

$2 \leq (x - 3) \leq 4 \text{ or } -4 \leq (x - 3) \leq -2$

$5 \leq x \leq 7 \text{ or } -1 \leq x \leq 1$

$A = \{-1, 0, 1, 5, 6, 7\}$

$B \Rightarrow x = 4, |x - 2| = 1 \Rightarrow x = 3 \text{ or } 1 (\text{reject}) +$

$B = \{4, 3\}$

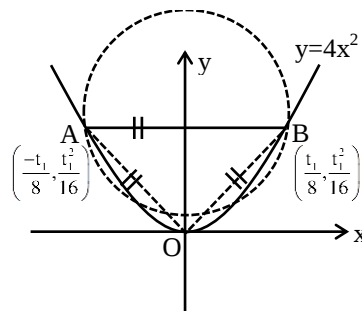
Number of onto functions from A to $B = 2^6 - 2 = 62$

15. An equilateral triangle OAB is inscribed in the parabola $y = 4x^2$ whose vertex is O . Find the least distance of the circle described on AB as diameter from the origin.

- (1) $\frac{6 - \sqrt{3}}{2}$ (2) $\frac{3 - \sqrt{3}}{4}$
(3) $\frac{6 + \sqrt{3}}{2}$ (4) $\frac{3 + \sqrt{3}}{2}$

Ans. (2)

Sol.



$OB^2 = AB^2$

$\Rightarrow \frac{t_1^2}{64} + \frac{t_1^4}{256} = \frac{t_1^2}{16}$

$\Rightarrow 4t_1^2 + t_1^4 = 16t_1^2$

$\Rightarrow t_1 = 2\sqrt{3}$

$\therefore A \left(\frac{-\sqrt{3}}{4}, \frac{3}{4} \right) \text{ \& } B \left(\frac{\sqrt{3}}{4}, \frac{3}{4} \right)$

Midpoint of AB i.e. centre of circle is $\left(0, \frac{3}{4} \right)$ and

radius = $\frac{\sqrt{3}}{4}$

$\therefore OP = OM - r = \frac{3}{4} - \frac{\sqrt{3}}{4} = \frac{3 - \sqrt{3}}{4}$

16. If the point of intersection of ellipses $x^2 + 2y^2 - 6x - 12y + 23 = 0$ and $4x^2 + 2y^2 - 20x - 12y + 35 = 0$ lie on a circle of radius r and centre (a, b) , then the value of $ab + 18r^2$ is

- (1) 90 (2) 95 (3) 85 (4) 100

Ans. (2)

Sol. $4x^2 + 2y^2 - 20x - 12y + 35 = 0$

$2(x^2 + 2y^2 - 6x - 12y + 23) = 0$

$6x^2 + 6y^2 - 32x - 36y + 81 = 0$

$x^2 + y^2 - \frac{16}{3}x - 6y + \frac{27}{2} = 0$

$(a, b) \equiv \left(\frac{8}{3}, 3 \right)$

$r = \sqrt{\frac{64}{9} + 9 - \frac{27}{2}} = \sqrt{\frac{87}{18}}$

$r^2 = \frac{87}{18} \Rightarrow 18r^2 = 87$

Now, $ab + 18r^2 = 8 + 87 = 95$



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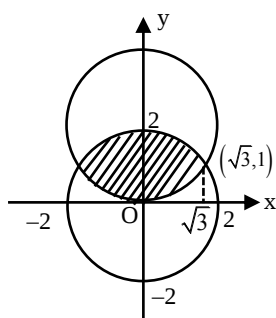
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17. Find the area bounded by the curves $x^2 + y^2 = 4$ & $x^2 + (y-2)^2 = 4$

- (1) $\frac{8\pi}{3} - 2\sqrt{3}$ Sq. units (2) $\frac{8\pi}{3} + \sqrt{3}$ Sq. units
(3) $\frac{4\pi}{3} - 2\sqrt{3}$ Sq. units (4) $\frac{4\pi}{3} + 2\sqrt{3}$ Sq. units

Ans. (1)

Sol.



$$\begin{aligned} A &= 2 \int_0^{\sqrt{3}} \left[\sqrt{4-x^2} - (2 - \sqrt{4-x^2}) \right] dx \\ &= 2 \int_0^{\sqrt{3}} (2\sqrt{4-x^2} - 2) dx \\ &= 4 \int_0^{\sqrt{3}} (\sqrt{4-x^2} - 1) dx \\ &= \left[4 \left[\frac{1}{2} \left(x\sqrt{4-x^2} + 4\sin^{-1} \frac{x}{2} \right) - x \right] \right]_0^{\sqrt{3}} \\ &= 4 \left[\frac{1}{2} \left(\sqrt{3} + 4 \times \frac{\pi}{3} \right) - \sqrt{3} \right] = 4 \left[\frac{2\pi}{3} - \frac{\sqrt{3}}{2} \right] \\ &= \frac{8\pi}{3} - 2\sqrt{3} \text{ (Sq. units)} \end{aligned}$$

18. If $z = \frac{\sqrt{3}}{2} + \frac{i}{2}$, then $(z^{201} - i)^8$ is -

- (1) 0 (2) 256
(3) 1 (4) -1

Ans. (2)

Sol. $z = \cos \frac{\pi}{6} + i \sin \frac{\pi}{6}$

$$z^{201} = \cos \left(201 \frac{\pi}{6} \right) + i \sin \left(201 \frac{\pi}{6} \right) = -i$$

$$(z^{201} - i)^8 = (-2i)^8 = 256$$

19. If $I(x) = 3 \int \frac{dx}{(4x+6)\sqrt{4x^2+8x+3}}$, $I(0) = \frac{\sqrt{3}}{4}$,

then $I(1) =$

- (1) $\frac{3\sqrt{15}}{20}$ (2) $\frac{3\sqrt{15}}{10}$
(3) $\frac{\sqrt{15}}{10}$ (4) $\frac{\sqrt{15}}{20}$

Ans. (1)

Sol. Let $4x+6 = \frac{1}{t}$

$$dx = \frac{-dt}{4t^2}$$

$$I = \frac{-3}{4} \int \frac{dt}{t^2 \times \frac{1}{t} \times \sqrt{4 \left(\frac{1-t}{t} \right)^2 + 2 \left(\frac{1-t}{t} \right) + 3}}$$

$$= \frac{-3}{4} \int \frac{dt}{t \sqrt{\frac{1}{4} \left(\frac{1-6t}{t} \right)^2 + \frac{2}{t} - 9}}$$

$$= \frac{-3}{2} \int \frac{dt}{\sqrt{1-4t}}$$

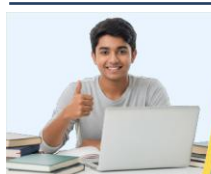
$$= \frac{-3}{2} \times \frac{-1}{4} \times \frac{(1-4t)^{\frac{1}{2}}}{\frac{1}{2}} + C$$

$$= \frac{3}{4} \sqrt{1-4t} + C = \frac{3}{4} \sqrt{1 - \frac{4}{4x+6}} + C$$

$$I(0) = \frac{3}{4} \sqrt{1 - \frac{2}{3}} + C = \frac{\sqrt{3}}{4} \Rightarrow C = 0$$

$$I(x) = \frac{3}{4} \sqrt{1 - \frac{4}{4x+6}}$$

$$\therefore I(1) = \frac{3}{4} \times \sqrt{\frac{6}{10}} = \frac{3\sqrt{6}}{4\sqrt{10}} = \frac{3\sqrt{60}}{40} = \frac{3\sqrt{15}}{20}$$



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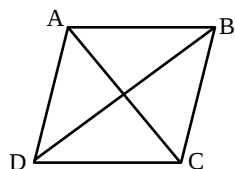
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20. Rhombus ABCD is given with vertices A(1,2), C(-3,-6) and sides AD & BC are parallel to the line $7x - y = 14$. If coordinates of B & C are (α, β) & (γ, δ) respectively, then find $\alpha + \beta + \gamma + \delta = ?$

- (1) -4 (2) 5
(3) -6 (4) -7

Ans. (3)

Sol. Mid points of BD & AC are same



$$\text{As } \frac{\alpha + \gamma}{2} = \frac{1 + (-3)}{2}, \frac{\beta + \delta}{2} = \frac{2 + (-6)}{2}$$

$$\alpha + \gamma = -2, \beta + \delta = -4$$

$$\alpha + \beta + \gamma + \delta = -6$$

21.

Class	4-8	8-12	12-16	16-20
Freq.(f _i)	3	λ	4	7

The mean and variance of following data is μ & 19 respectively & μ is an integer. The value of $(\lambda + \mu)$ is

- (1) 19 (2) 20
(3) 13 (4) 17

Ans. (1)

$$\text{Sol. } \mu = \frac{\sum f_i x_i}{\sum f_i} = \frac{18 + 10\lambda + 56 + 126}{14 + \lambda}$$

$$= \frac{200 + 10\lambda}{\lambda + 14} = 10 + \left(\frac{60}{\lambda + 14} \right)$$

$\lambda + 14$ is multiply of 60 $\Rightarrow \lambda = 1$ or 6 or 16.

$$\sigma^2 = \frac{\sum x_i^2}{\lambda + 14} - (\mu)^2$$

$$\sigma^2 = \frac{6^2(3) + 10^2(\lambda) + 14^2(4) + (18)^2(7)}{\lambda + 14} - \mu^2$$

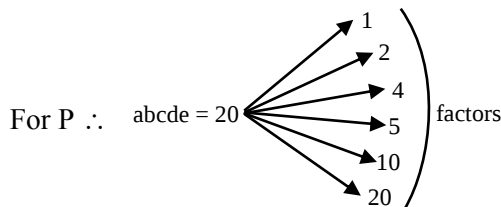
$$\text{for } \lambda = 6, \mu = 10 + 3 = 13$$

$$\lambda + \mu = 19$$

22. Let S = number of 4 digit numbers abcd, where $a > b > c > d$ & P = number of 5 digit numbers abcde, where product of digits is 20, then $S + P =$

Ans. (260)

$$\text{Sol. } S = {}^{10}C_4 = 210$$



$$\therefore \text{Case -(1)} \quad 5 \ 4 \ 1 \ 1 \ 1 \Rightarrow \frac{5!}{3!} = 20$$

$$\text{Case -(2)} \quad 5 \ 2 \ 2 \ 1 \ 1 \Rightarrow \frac{5!}{2!2!} = 30$$

$$\therefore P = 20 + 30 = 50$$

$$\therefore S + P = 260$$

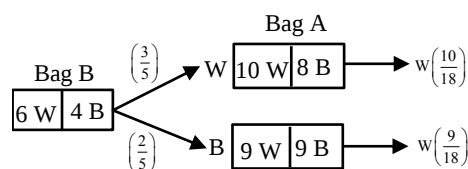
23. Bag A contains 9 White & 8 Black balls and bag B contains 6 White & 4 Black balls. A ball is randomly transferred from bag B to bag A then a ball is drawn from bag A. If probability that drawn

ball is White, is $\frac{p}{q}$ (Where p & q are coprime),

then $(p + q)$ is

Ans. (23)

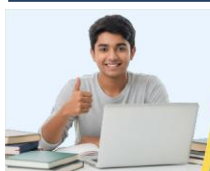
Sol.



$$\therefore P(\text{Drawn ball is white}) = \frac{3}{5} \times \frac{10}{18} + \frac{2}{5} \times \frac{9}{18}$$

$$= \frac{48}{90} = \frac{8}{15} = \frac{p}{q}$$

$$\therefore p + q = 23$$



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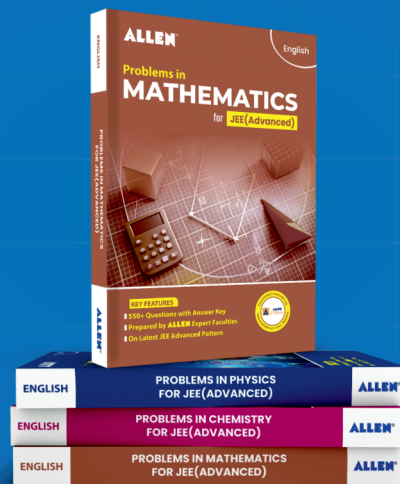
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